Package: sharp (via r-universe)

August 31, 2024

Type Package

Title Stability-enHanced Approaches using Resampling Procedures Version 1.4.6 Date 2024-02-03 Author Barbara Bodinier [aut, cre] Maintainer Barbara Bodinier
barbara.bodinier@gmail.com> URL <https://github.com/barbarabodinier/sharp> BugReports <https://github.com/barbarabodinier/sharp/issues> Description In stability selection (N Meinshausen, P Bühlmann (2010) $\langle \text{doi:10.1111/j.1467-9868.2010.00740.x} \rangle$ and consensus clustering (S Monti et al (2003) [<doi:10.1023/A:1023949509487>](https://doi.org/10.1023/A:1023949509487)), resampling techniques are used to enhance the reliability of the results. In this package, hyper-parameters are calibrated by maximising model stability, which is measured under the null hypothesis that all selection (or co-membership) probabilities are identical (B Bodinier et al (2023a) [<doi:10.1093/jrsssc/qlad058>](https://doi.org/10.1093/jrsssc/qlad058) and B Bodinier et al (2023b) [<doi:10.1093/bioinformatics/btad635>](https://doi.org/10.1093/bioinformatics/btad635)). Functions are readily implemented for the use of LASSO regression, sparse PCA, sparse (group) PLS or graphical LASSO in stability selection, and hierarchical clustering, partitioning around medoids, K means or Gaussian mixture models in consensus clustering.

License GPL $(>= 3)$

Language en-GB

Encoding UTF-8

RoxygenNote 7.3.1

Depends fake $(>= 1.4.0)$, R $(>= 3.5)$

Imports abind, beepr, future, future.apply, glassoFast (>= 1.0.0), glmnet, grDevices, igraph, mclust, nloptr, plotrix, Rdpack, with $(>= 2.4.0)$

2 Contents

Suggests cluster, corpcor, dbscan, elasticnet, gglasso, mixOmics, nnet, OpenMx, RCy3, randomcoloR, rCOSA, rmarkdown, rpart, sgPLS, sparcl, survival $(>= 3.2.13)$, testthat $(>= 3.0.0)$, visNetwork

Additional_repositories <https://barbarabodinier.github.io/drat>

Config/testthat/edition 3

RdMacros Rdpack

Repository https://barbarabodinier.r-universe.dev

RemoteUrl https://github.com/barbarabodinier/sharp

RemoteRef HEAD

RemoteSha d2cc3d9bc64561b9deb7c2311bb130e561e4f2ab

Contents

sharp-package *sharp: Stability-enHanced Approaches using Resampling Procedures*

Description

In stability selection and consensus clustering, resampling techniques are used to enhance the reliability of the results. In this package, hyper-parameters are calibrated by maximising model stability, which is measured under the null hypothesis that all selection (or co-membership) probabilities are identical. Functions are readily implemented for the use of LASSO regression, sparse PCA, sparse (group) PLS or graphical LASSO in stability selection, and hierarchical clustering, partitioning around medoids, K means or Gaussian mixture models in consensus clustering.

Details

References

Bodinier B, Vuckovic D, Rodrigues S, Filippi S, Chiquet J, Chadeau-Hyam M (2023). "Automated calibration of consensus weighted distance-based clustering approaches using sharp." *Bioinformatics*, btad635. ISSN 1367-4811, [doi:10.1093/bioinformatics/btad635,](https://doi.org/10.1093/bioinformatics/btad635) https://academic.oup.com/bioinformatics/advancearticle-pdf/doi/10.1093/bioinformatics/btad635/52191190/btad635.pdf.

Bodinier B, Filippi S, Nøst TH, Chiquet J, Chadeau-Hyam M (2023). "Automated calibration for stability selection in penalised regression and graphical models." *Journal of the Royal Statistical Society Series C: Applied Statistics*, qlad058. ISSN 0035-9254, [doi:10.1093/jrsssc/qlad058,](https://doi.org/10.1093/jrsssc/qlad058) https://academic.oup.com/jrsssc/advance-article-pdf/doi/10.1093/jrsssc/qlad058/50878777/qlad058.pdf.

Meinshausen N, Bühlmann P (2010). "Stability selection." *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 72(4), 417-473. [doi:10.1111/j.14679868.2010.00740.x.](https://doi.org/10.1111/j.1467-9868.2010.00740.x)

Monti S, Tamayo P, Mesirov J, Golub T (2003). "Consensus Clustering: A Resampling-Based Method for Class Discovery and Visualization of Gene Expression Microarray Data." *Machine Learning*, 52(1), 91–118. [doi:10.1023/A:1023949509487.](https://doi.org/10.1023/A%3A1023949509487)

```
oldpar <- par(no.readonly = TRUE)
par(max = c(5, 5, 5, 5))## Regression models
# Data simulation
set.seed(1)
simul <- SimulateRegression(n = 100, pk = 50)
# Stability selection
stab <- VariableSelection(xdata = simul$xdata, ydata = simul$ydata)
CalibrationPlot(stab)
summary(stab)
SelectedVariables(stab)
## Graphical models
# Data simulation
set.seed(1)
simul <- SimulateGraphical(n = 100, pk = 20, topology = "scale-free")
```

```
# Stability selection
stab <- GraphicalModel(xdata = simul$data)
CalibrationPlot(stab)
summary(stab)
plot(stab)
## PCA models
if (requireNamespace("elasticnet", quietly = TRUE)) {
  # Data simulation
  set.seed(1)
  simul <- SimulateComponents(pk = c(5, 3, 4))
  plot(simul)
  # Stability selection
  stab <- BiSelection(
   xdata = simul$data,
   ncomp = 3,
   implementation = SparsePCA
  )
  CalibrationPlot(stab)
  summary(stab)
  SelectedVariables(stab)
}
## PLS models
if (requireNamespace("sgPLS", quietly = TRUE)) {
  # Data simulation
  set.seed(1)
  simul \le SimulateRegression(n = 50, pk = c(10, 20, 30), family = "gaussian")
  # Stability selection
  stab <- BiSelection(
   xdata = simul$xdata, ydata = simul$ydata,
   family = "gaussian", ncomp = 3,
    implementation = SparsePLS
  \lambdaCalibrationPlot(stab)
  summary(stab)
  plot(stab)
}
par(oldpar)
```
AggregatedEffects *Summarised coefficients conditionally on selection*

Description

Computes descriptive statistics (defined by FUN) for coefficients of the (calibrated) models conditionally on selection across resampling iterations.

Usage

```
AggregatedEffects(
  stability,
  lambda_id = NULL,
  side = "X",comp = 1,FUN = stats::median,
  ...
\lambda
```
Arguments

Value

A matrix of summarised coefficients conditionally on selection across resampling iterations. Missing values (NA) are returned for variables that are never selected.

See Also

[VariableSelection](#page-117-1), [BiSelection](#page-7-1), [Refit](#page-87-1)

```
# Example with univariate outcome
set.seed(1)
simul <- SimulateRegression(n = 100, pk = 50, family = "gaussian")
stab <- VariableSelection(xdata = simul$xdata, ydata = simul$ydata, family = "gaussian")
median_betas <- AggregatedEffects(stab)
# Comparison with refitted model
refitted <- Refit(xdata = simul$xdata, ydata = simul$ydata, stability = stab)
refitted_betas <- coef(refitted)[-1, 1]
plot(median_betas[names(refitted_betas), ], refitted_betas,
```
ArgmaxId 7

```
panel.first = abline(0, 1, 1ty = 2))
# Extracting mean betas conditionally on selection
mean_betas <- AggregatedEffects(stab, FUN = mean)
plot(median_betas, mean_betas)
# Regression with multivariate outcomes
set.seed(1)
simul <- SimulateRegression(n = 100, pk = 50, q = 2, family = "gaussian")
stab <- VariableSelection(xdata = simul$xdata, ydata = simul$ydata, family = "mgaussian")
median_betas <- AggregatedEffects(stab)
dim(median_betas)
# Sparse PLS with multivariate outcome
if (requireNamespace("sgPLS", quietly = TRUE)) {
 set.seed(1)
 simul \le SimulateRegression(n = 50, pk = 15, q = 3, family = "gaussian")
 x <- simul$xdata
 y <- simul$ydata
 stab <- BiSelection(
   xdata = x, ydata = y,
   family = "gaussian", ncomp = 3,
   LambdaX = seq\_len(ncol(x) - 1),
   implementation = SparsePLS
 )
 median_betas <- AggregatedEffects(stab)
 dim(median_betas)
 median_betas <- AggregatedEffects(stab, side = "Y")
 dim(median_betas)
}
```


ArgmaxId *Calibrated hyper-parameter(s)*

Description

Extracts the calibrated hyper-parameters (or their indices for [ArgmaxId](#page-6-1)) with respect to the grids provided in Lambda and pi_list in argument stability.

Usage

 $ArgmaxId(statility = NULL, S = NULL)$

Argmax(stability)

Arguments

Value

A matrix of hyper-parameters ([Argmax](#page-6-2)) or indices ([ArgmaxId](#page-6-1)). For multi-block graphical models, rows correspond to different blocks.

See Also

[VariableSelection](#page-117-1), [GraphicalModel](#page-45-1)

Examples

```
# Data simulation
set.seed(1)
simul <- SimulateGraphical(pk = 20)
# Stability selection
stab <- GraphicalModel(xdata = simul$data)
# Extracting calibrated hyper-parameters
Argmax(stab)
# Extracting calibrated hyper-parameters IDs
ids <- ArgmaxId(stab)
ids
# Relationship between the two functions
stab$Lambda[ids[1], 1]
stab$params$pi_list[ids[2]]
```
BiSelection *Stability selection of predictors and/or outcomes*

Description

Performs stability selection for dimensionality reduction. The underlying variable selection algorithm (e.g. sparse PLS) is run with different combinations of parameters controlling the sparsity (e.g. number of selected variables per component) and thresholds in selection proportions. These hyper-parameters are jointly calibrated by maximisation of the stability score.

BiSelection 9

Usage

```
BiSelection(
 xdata,
 ydata = NULL,
 group_x = NULL,group_y = NULL,LambdaX = NULL,LambdaY = NULL,
 AlphaX = NULL,AlphaY = NULL,
 ncomp = 1,
 scale = TRUE,pi_list = seq(0.01, 0.99, by = 0.01),K = 100,tau = 0.5,
  seed = 1,
 n_{cat} = NULL,
  family = "gaussian",
  implementation = SparsePLS,
  resampling = "subsampling",
  cpss = FALSE,PFER_method = "MB",
 PFER_thr = Inf,
 FDP_{thr} = Inf,n\_cores = 1,output_data = FALSE,
  verbose = TRUE,
 beep = NULL,...
\mathcal{L}
```
Arguments

BiSelection 11

Details

In stability selection, a feature selection algorithm is fitted on K subsamples (or bootstrap samples) of the data with different parameters controlling the sparsity (LambdaX, LambdaY, AlphaX, and/or AlphaY). For a given (set of) sparsity parameter(s), the proportion out of the K models in which each feature is selected is calculated. Features with selection proportions above a threshold pi are considered stably selected. The stability selection model is controlled by the sparsity parameter(s) (denoted by λ) for the underlying algorithm, and the threshold in selection proportion:

 $V_{\lambda,\pi} = \{j : p_{\lambda}(j) \geq \pi\}$

For sparse and sparse group dimensionality reduction, "feature" refers to variable (variable selection model). For group PLS, "feature" refers to group (group selection model). For (sparse) group PLS, groups need to be defined *a priori* and specified in arguments group_x and/or group_y.

These parameters can be calibrated by maximisation of a stability score (see [ConsensusScore](#page-28-1) if n_cat=NULL or [StabilityScore](#page-109-1) otherwise) calculated under the null hypothesis of equiprobability of selection.

It is strongly recommended to examine the calibration plot carefully to check that the grids of parameters Lambda and pi_list do not restrict the calibration to a region that would not include the global maximum (see [CalibrationPlot](#page-15-1)). In particular, the grid Lambda may need to be extended when the maximum stability is observed on the left or right edges of the calibration heatmap. In some instances, multiple peaks of stability score can be observed. Simulation studies suggest that the peak corresponding to the largest number of selected features tend to give better selection performances. This is not necessarily the highest peak (which is automatically retained by the functions in this package). The user can decide to manually choose another peak.

To control the expected number of False Positives (Per Family Error Rate) in the results, a threshold PFER_thr can be specified. The optimisation problem is then constrained to sets of parameters that generate models with an upper-bound in PFER below PFER_thr (see Meinshausen and Bühlmann (2010) and Shah and Samworth (2013)).

Possible resampling procedures include defining (i) K subsamples of a proportion tau of the observations, (ii) K bootstrap samples with the full sample size (obtained with replacement), and (iii) K/2 splits of the data in half for complementary pair stability selection (see arguments resampling and cpss). In complementary pair stability selection, a feature is considered selected at a given resampling iteration if it is selected in the two complementary subsamples.

For categorical outcomes (argument family is "binomial" or "multinomial"), the proportions of observations from each category in all subsamples or bootstrap samples are the same as in the full sample.

To ensure reproducibility of the results, the starting number of the random number generator is set to seed.

For parallelisation, stability selection with different sets of parameters can be run on n_cores cores. Using n_cores > 1 creates a [multisession](#page-0-0).

Value

An object of class bi_selection. A list with:

BiSelection 13

The rows of summary and columns of selectedX, selectedY, selpropX, selpropY, selected, coefX and coefY are ordered in the same way and correspond to components and parameter values stored in summary. The rows of summary_full and columns of selectedX_full, selectedY_full, selpropX_full and selpropY_full are ordered in the same way and correspond to components and parameter values stored in summary_full.

References

Bodinier B, Filippi S, Nøst TH, Chiquet J, Chadeau-Hyam M (2023). "Automated calibration for stability selection in penalised regression and graphical models." *Journal of the Royal Statistical Society Series C: Applied Statistics*, qlad058. ISSN 0035-9254, [doi:10.1093/jrsssc/qlad058,](https://doi.org/10.1093/jrsssc/qlad058) https://academic.oup.com/jrsssc/advance-article-pdf/doi/10.1093/jrsssc/qlad058/50878777/qlad058.pdf.

Shah RD, Samworth RJ (2013). "Variable selection with error control: another look at stability selection." *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 75(1), 55- 80. [doi:10.1111/j.14679868.2011.01034.x.](https://doi.org/10.1111/j.1467-9868.2011.01034.x)

Meinshausen N, Bühlmann P (2010). "Stability selection." *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 72(4), 417-473. [doi:10.1111/j.14679868.2010.00740.x.](https://doi.org/10.1111/j.1467-9868.2010.00740.x)

Liquet B, de Micheaux PL, Hejblum BP, Thiébaut R (2016). "Group and sparse group partial least square approaches applied in genomics context." *Bioinformatics*, 32(1), 35-42. ISSN 1367-4803, [doi:10.1093/bioinformatics/btv535.](https://doi.org/10.1093/bioinformatics/btv535)

KA LC, Rossouw D, Robert-Granié C, Besse P (2008). "A sparse PLS for variable selection when integrating omics data." *Stat Appl Genet Mol Biol*, 7(1), Article 35. ISSN 1544-6115, [doi:10.2202/](https://doi.org/10.2202/1544-6115.1390) [15446115.1390.](https://doi.org/10.2202/1544-6115.1390)

Shen H, Huang JZ (2008). "Sparse principal component analysis via regularized low rank matrix approximation." *Journal of Multivariate Analysis*, 99(6), 1015-1034. ISSN 0047-259X, [doi:10.1016/](https://doi.org/10.1016/j.jmva.2007.06.007) [j.jmva.2007.06.007.](https://doi.org/10.1016/j.jmva.2007.06.007)

Zou H, Hastie T, Tibshirani R (2006). "Sparse Principal Component Analysis." *Journal of Computational and Graphical Statistics*, 15(2), 265-286. [doi:10.1198/106186006X113430.](https://doi.org/10.1198/106186006X113430)

See Also

[SparsePCA](#page-100-1), [SparsePLS](#page-102-1), [GroupPLS](#page-52-1), [SparseGroupPLS](#page-98-1), [VariableSelection](#page-117-1), [Resample](#page-90-1), [StabilityScore](#page-109-1) Other stability functions: [Clustering\(](#page-19-1)), [GraphicalModel\(](#page-45-1)), [StructuralModel\(](#page-112-1)), [VariableSelection\(](#page-117-1))

```
if (requireNamespace("sgPLS", quietly = TRUE)) {
 oldpar <- par(no.readonly = TRUE)
 par(max = c(12, 5, 1, 1))## Sparse Principal Component Analysis
 # Data simulation
 set.seed(1)
 simul <- SimulateComponents(pk = c(5, 3, 4))
 # sPCA: sparsity on X (unsupervised)
 stab <- BiSelection(
```

```
xdata = simul$data,
  ncomp = 2,
 LambdaX = seq\_len(ncol(simul$data) - 1),
 implementation = SparsePCA
\lambdaprint(stab)
# Calibration plot
CalibrationPlot(stab)
# Visualisation of the results
summary(stab)
plot(stab)
SelectedVariables(stab)
## Sparse (Group) Partial Least Squares
# Data simulation (continuous outcomes)
set.seed(1)
simul \le SimulateRegression(n = 100, pk = 15, q = 3, family = "gaussian")
x <- simul$xdata
y <- simul$ydata
# sPLS: sparsity on X
stab <- BiSelection(
 xdata = x, ydata = y,
 family = "gaussian", ncomp = 3,
 LambdaX = seq\_len(ncol(x) - 1),
 implementation = SparsePLS
)
CalibrationPlot(stab)
summary(stab)
plot(stab)
# sPLS: sparsity on both X and Y
stab <- BiSelection(
 xdata = x, ydata = y,
  family = "gaussian", ncomp = 3,
 LambdaX = seq\_len(ncol(x) - 1),
 LambdaY = seq\_len(ncol(y) - 1),
 implementation = SparsePLS,
 n_{cat} = 2)
CalibrationPlot(stab)
summary(stab)
plot(stab)
# sgPLS: sparsity on X
stab <- BiSelection(
 xdata = x, ydata = y, K = 10,
  group_x = c(2, 8, 5),family = "gaussian", ncomp = 3,
```
BlockLambdaGrid 15

```
LambdaX = seq\_len(2), AlphaX = seq(0.1, 0.9, by = 0.1),
   implementation = SparseGroupPLS
 )
 CalibrationPlot(stab)
 summary(stab)
 par(oldpar)
}
```
BlockLambdaGrid *Multi-block grid*

Description

Generates a matrix of parameters controlling the sparsity of the underlying selection algorithm for multi-block calibration.

Usage

BlockLambdaGrid(Lambda, lambda_other_blocks = NULL)

Arguments

Lambda vector or matrix of penalty parameters.

lambda_other_blocks

optional vector of penalty parameters to use for other blocks in the iterative multi-block procedure.

Value

See Also

[GraphicalModel](#page-45-1)

Examples

```
# Multi-block grid
Lambda <- matrix(
  c(
    0.8, 0.6, 0.3,
    0.5, 0.4, 0.2,
    0.7, 0.5, 0.1
  ),
  ncol = 3, byrow = TRUE
)
mygrid <- BlockLambdaGrid(Lambda, lambda_other_blocks = 0.1)
# Multi-parameter grid (not recommended)
Lambda <- matrix(
  c(
    0.8, 0.6, 0.3,
    0.5, 0.4, 0.2,
    0.7, 0.5, 0.1
  ),
  ncol = 3, byrow = TRUE
\mathcal{L}mygrid <- BlockLambdaGrid(Lambda, lambda_other_blocks = NULL)
```
CalibrationPlot *Calibration plot*

Description

Creates a plot showing the stability score as a function of the parameter(s) controlling the level of sparsity in the underlying feature selection algorithm and/or the threshold in selection proportions. See examples in [VariableSelection](#page-117-1), [GraphicalModel](#page-45-1), [Clustering](#page-19-1) and [BiSelection](#page-7-1).

Usage

```
CalibrationPlot(
  stability,
  block_id = NULL,col = NULL,pch = 19,
  cex = 0.7,
  xlim = NULL,ylim = NULL,
  bty = "o",lines = TRUE,
  lty = 3.
  1wd = 2,
  show_{\text{argmax}} = \text{TRUE},
  show\_pix = FALSE,
```


CalibrationPlot 17

```
show\_piy = FALSE,offset = 0.3,
 legend = TRUE,legend_length = NULL,
 legend_range = NULL,
 ncol = 1,
 xlab = NULL,
 ylab = NULL,
 zlab = expression(italic(q)),xlas = 2,
 ylas = NULL,
 zlas = 2,
 cex.1ab = 1.5,
 cex. axis = 1,cex. legend = 1.2,xgrid = FALSE,
 ygrid = FALSE,
 params = c("ny", "alphay", "nx", "alphax")
\mathcal{L}
```
Arguments

Value

A calibration plot.

See Also

[VariableSelection](#page-117-1), [GraphicalModel](#page-45-1), [Clustering](#page-19-1), [BiSelection](#page-7-1)

 $Classification$ *And Regression Trees*

Description

Runs decision trees using implementation from [rpart](#page-0-0). This function is not using stability.

$CART$ 19

Usage

CART(xdata, ydata, Lambda = NULL, family, ...)

Arguments

Value

A list with:

References

Breiman L, Friedman JH, Olshen R, Stone CJ (1984). *Classification and Regression Trees*. Wadsworth.

See Also

[SelectionAlgo](#page-92-1), [VariableSelection](#page-117-1)

Other underlying algorithm functions: [ClusteringAlgo\(](#page-23-1)), [PenalisedGraphical\(](#page-70-1)), [PenalisedOpenMx\(](#page-72-1)), [PenalisedRegression\(](#page-74-1))

```
if (requireNamespace("rpart", quietly = TRUE)) {
 # Data simulation
 set.seed(1)
 simul <- SimulateRegression(pk = 50)
 # Running the LASSO
 mycart <- CART(
   xdata = simul$xdata,
   ydata = simul$ydata,
   family = "gaussian"
 )
```

```
head(mycart$selected)
}
```
Clustering *Consensus clustering*

Description

Performs consensus (weighted) clustering. The underlying algorithm (e.g. hierarchical clustering) is run with different number of clusters nc. In consensus weighed clustering, weighted distances are calculated using the [cosa2](#page-0-0) algorithm with different penalty parameters Lambda. The hyperparameters are calibrated by maximisation of the consensus score.

Usage

```
Clustering(
  xdata,
  nc = NULL,eps = NULL,
 Lambda = NULL,K = 100,
  tau = 0.5,
  seed = 1,
  n_{cat} = 3,
  implementation = HierarchicalClustering,
  scale = TRUE,
  linkage = "complete",
  row = TRUE,
  optimisation = c("grid_search", "nloptr"),
  n\_cores = 1,output_data = FALSE,
  verbose = TRUE,
  beep = NULL,
  ...
)
```
Arguments

Details

In consensus clustering, a clustering algorithm is applied on K subsamples of the observations with different numbers of clusters provided in nc. If row=TRUE (the default), the observations (rows) are the items to cluster. If row=FALSE, the variables (columns) are the items to cluster. For a given number of clusters, the consensus matrix coprop stores the proportion of iterations where

two items were in the same estimated cluster, out of all iterations where both items were drawn in the subsample.

Stable cluster membership is obtained by applying a distance-based clustering method using (1-coprop) as distance (see [Clusters\)](#page-110-1).

These parameters can be calibrated by maximisation of a stability score (see [ConsensusScore](#page-28-1)) calculated under the null hypothesis of equiprobability of co-membership.

It is strongly recommended to examine the calibration plot (see [CalibrationPlot](#page-15-1)) to check that there is a clear maximum. The absence of a clear maximum suggests that the clustering is not stable, consensus clustering outputs should not be trusted in that case.

To ensure reproducibility of the results, the starting number of the random number generator is set to seed.

For parallelisation, stability selection with different sets of parameters can be run on n_cores cores. Using n_cores > 1 creates a [multisession](#page-0-0).

Value

An object of class clustering. A list with:

The rows of Sc, nc, Lambda, Q, selprop and indices along the third dimension of coprop are ordered in the same way and correspond to parameter values stored in nc and Lambda.

References

Bodinier B, Vuckovic D, Rodrigues S, Filippi S, Chiquet J, Chadeau-Hyam M (2023). "Automated calibration of consensus weighted distance-based clustering approaches using sharp." *Bioinformatics*, btad635. ISSN 1367-4811, [doi:10.1093/bioinformatics/btad635,](https://doi.org/10.1093/bioinformatics/btad635) https://academic.oup.com/bioinformatics/advancearticle-pdf/doi/10.1093/bioinformatics/btad635/52191190/btad635.pdf.

Clustering 23

Kampert MM, Meulman JJ, Friedman JH (2017). "rCOSA: A Software Package for Clustering Objects on Subsets of Attributes." *Journal of Classification*, 34(3), 514–547. [doi:10.1007/s00357-](https://doi.org/10.1007/s00357-017-9240-z) [0179240z.](https://doi.org/10.1007/s00357-017-9240-z)

Friedman JH, Meulman JJ (2004). "Clustering objects on subsets of attributes (with discussion)." *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 66(4), 815-849. [doi:10.1](https://doi.org/10.1111/j.1467-9868.2004.02059.x)111/ [j.14679868.2004.02059.x,](https://doi.org/10.1111/j.1467-9868.2004.02059.x) https://rss.onlinelibrary.wiley.com/doi/pdf/10.1111/j.1467-9868.2004.02059.x, <https://rss.onlinelibrary.wiley.com/doi/abs/10.1111/j.1467-9868.2004.02059.x>.

Monti S, Tamayo P, Mesirov J, Golub T (2003). "Consensus Clustering: A Resampling-Based Method for Class Discovery and Visualization of Gene Expression Microarray Data." *Machine Learning*, 52(1), 91–118. [doi:10.1023/A:1023949509487.](https://doi.org/10.1023/A%3A1023949509487)

See Also

[Resample](#page-90-1), [ConsensusScore](#page-28-1), [HierarchicalClustering](#page-54-1), [PAMClustering](#page-69-1), [KMeansClustering](#page-59-1), [GMMClustering](#page-39-1)

Other stability functions: [BiSelection\(](#page-7-1)), [GraphicalModel\(](#page-45-1)), [StructuralModel\(](#page-112-1)), [VariableSelection\(](#page-117-1))

```
# Consensus clustering
set.seed(1)
simul <- SimulateClustering(
 n = c(30, 30, 30), nu\_xc = 1, ev\_xc = 0.5\mathcal{L}stab <- Clustering(xdata = simul$data)
print(stab)
CalibrationPlot(stab)
summary(stab)
Clusters(stab)
plot(stab)
# Consensus weighted clustering
if (requireNamespace("rCOSA", quietly = TRUE)) {
  set.seed(1)
  simul <- SimulateClustering(
    n = c(30, 30, 30), pk = 20,
    theta_xc = c(rep(1, 10), rep(0, 10)),ev_{\text{c}}xc = 0.9
  )
  stab <- Clustering(
    xdata = simul$data,
    Lambda = LambdaSequence(lmin = 0.1, lmax = 10, cardinal = 10),
    noit = 20, niter = 10
  \lambdaprint(stab)
  CalibrationPlot(stab)
  summary(stab)
  Clusters(stab)
  plot(stab)
  WeightBoxplot(stab)
}
```
ClusteringAlgo *(Weighted) clustering algorithm*

Description

Runs the (weighted) clustering algorithm specified in the argument implementation and returns matrices of variable weights, and the co-membership structure. This function is not using stability.

Usage

```
ClusteringAlgo(
 xdata,
 nc = NULL,eps = NULL,
 Lambda = NULL,
  scale = TRUE,
  row = TRUE,
  implementation = HierarchicalClustering,
  ...
)
```
Arguments

Value

A list with:

See Also

[VariableSelection](#page-117-1)

Other underlying algorithm functions: [CART\(](#page-17-1)), [PenalisedGraphical\(](#page-70-1)), [PenalisedOpenMx\(](#page-72-1)), [PenalisedRegression\(](#page-74-1))

Examples

```
# Simulation of 15 observations belonging to 3 groups
set.seed(1)
simul <- SimulateClustering(
  n = c(5, 5, 5), pk = 100
)
# Running hierarchical clustering
myclust <- ClusteringAlgo(
  xdata = simul$data, nc = 2:5,implementation = HierarchicalClustering
)
```
ClusteringPerformance *Clustering performance*

Description

Computes different metrics of clustering performance by comparing true and predicted co-membership. This function can only be used in simulation studies (i.e. when the true cluster membership is known).

Usage

```
ClusteringPerformance(theta, theta_star, ...)
```
Arguments

Value

A matrix of selection metrics including:

See Also

Other functions for model performance: [SelectionPerformance\(](#page-94-1)), [SelectionPerformanceGraph\(](#page-95-1))

```
# Data simulation
set.seed(1)
simul <- SimulateClustering(
 n = c(30, 30, 30), nu\_xc = 1)
plot(simul)
# Consensus clustering
stab <- Clustering(
 xdata = simul$data, nc = seq_len(5)
)
# Clustering performance
ClusteringPerformance(stab, simul)
```
Combine 27

```
# Alternative formulation
ClusteringPerformance(
  theta = CoMembership(Clusters(stab)),
  theta_star = simul$theta
)
```
Combine *Merging stability selection outputs*

Description

Merges the outputs from two runs of [VariableSelection](#page-117-1), [GraphicalModel](#page-45-1) or [Clustering](#page-19-1). The two runs must have been done using the same methods and the same params but with different seeds. The combined output will contain results based on iterations from both stability1 and stability2. This function can be used for parallelisation.

Usage

Combine(stability1, stability2, include_beta = TRUE)

Arguments

Value

A single output of the same format.

See Also

[VariableSelection](#page-117-1), [GraphicalModel](#page-45-1)

```
## Variable selection
# Data simulation
set.seed(1)
simul <- SimulateRegression(n = 100, pk = 50, family = "gaussian")
# Two runs
stab1 <- VariableSelection(xdata = simul$xdata, ydata = simul$ydata, seed = 1, K = 10)
stab2 <- VariableSelection(xdata = simul$xdata, ydata = simul$ydata, seed = 2, K = 10)
```

```
# Merging the outputs
stab <- Combine(stability1 = stab1, stability2 = stab2, include_beta = FALSE)
str(stab)
## Graphical modelling
# Data simulation
simul <- SimulateGraphical(pk = 20)
# Two runs
stab1 <- GraphicalModel(xdata = simul$data, seed = 1, K = 10)
stab2 <- GraphicalModel(xdata = simul$data, seed = 2, K = 10)
# Merging the outputs
stab <- Combine(stability1 = stab1, stability2 = stab2)
str(stab)
## Clustering
# Data simulation
simul <- SimulateClustering(n = c(15, 15, 15))
# Two runs
stab1 <- Clustering(xdata = simul$data, seed = 1)
stab2 <- Clustering(xdata = simul$data, seed = 2)
# Merging the outputs
stab <- Combine(stability1 = stab1, stability2 = stab2)
str(stab)
```
CoMembership *Pairwise co-membership*

Description

Generates a symmetric and binary matrix indicating, if two items are co-members, i.e. belong to the same cluster.

Usage

CoMembership(groups)

Arguments

groups vector of group membership.

ConsensusScore 29

Value

A symmetric and binary matrix.

Examples

```
# Simulated grouping structure
mygroups <- c(rep(1, 3), rep(2, 5), rep(3, 2))
```

```
# Co-membership matrix
CoMembership(mygroups)
```
ConsensusScore *Consensus score*

Description

Computes the consensus score from the consensus matrix, matrix of co-sampling counts and consensus clusters. The score is a z statistic for the comparison of the co-membership proportions observed within and between the consensus clusters.

Usage

ConsensusScore(prop, K, theta)

Arguments

Details

To calculate the consensus score, the features are classified as being stably selected or not (in selection) or as being in the same consensus cluster or not (in clustering). In selection, the quantities X_w and X_b are defined as the sum of the selection counts for features that are stably selected or not, respectively. In clustering, the quantities X_w and X_b are defined as the sum of the co-membership counts for pairs of items in the same consensus cluster or in different consensus clusters, respectively.

Conditionally on this classification, and under the assumption that the selection (or co-membership) probabilities are the same for all features (or item pairs) in each of these two categories, the quantities X_w and X_b follow binomial distributions with probabilities p_w and p_b , respectively.

In the most unstable situation, we suppose that all features (or item pairs) would have the same probability of being selected (or co-members). The consensus score is the z statistic from a z test where the null hypothesis is $p_w \leq p_b$.

The consensus score increases with stability.

Value

A consensus score.

See Also

Other stability metric functions: [FDP\(](#page-37-1)), [PFER\(](#page-76-1)), [StabilityMetrics\(](#page-105-1)), [StabilityScore\(](#page-109-1))

Examples

```
# Data simulation
set.seed(2)
simul <- SimulateClustering(
  n = c(30, 30, 30),
 nu_xc = 1\lambdaplot(simul)
# Consensus clustering
stab <- Clustering(
  xdata = simul$data
)
stab$Sc[3]
# Calculating the consensus score
theta <- CoMembership(Clusters(stab, argmax_id = 3))
ConsensusScore(
  prop = (stab$coprop[, , 3])[upper.tri(stab$coprop[, , 3])],
  K = stab$sampled_pairs[upper.tri(stab$sampled_pairs)],
  theta = theta[upper.tri(theta)]
)
```
DBSCANClustering *(Weighted) density-based clustering*

Description

Runs Density-Based Spatial Clustering of Applications with Noise (DBSCAN) clustering using implementation from [dbscan](#page-0-0). This is also known as the k-medoids algorithm. If Lambda is provided, clustering is applied on the weighted distance matrix calculated using the COSA algorithm as implemented in [cosa2](#page-0-0). Otherwise, distances are calculated using [dist](#page-0-0). This function is not using stability.

Usage

```
DBSCANClustering(
 xdata,
  nc = NULL,eps = NULL,
```


```
Lambda = NULL,
  distance = "euclidean",
  ...
\mathcal{L}
```
Arguments

Value

A list with:

References

Kampert MM, Meulman JJ, Friedman JH (2017). "rCOSA: A Software Package for Clustering Objects on Subsets of Attributes." *Journal of Classification*, 34(3), 514–547. [doi:10.1007/s00357-](https://doi.org/10.1007/s00357-017-9240-z) [0179240z.](https://doi.org/10.1007/s00357-017-9240-z)

Friedman JH, Meulman JJ (2004). "Clustering objects on subsets of attributes (with discussion)." *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 66(4), 815-849. [doi:10.1](https://doi.org/10.1111/j.1467-9868.2004.02059.x)111/ [j.14679868.2004.02059.x,](https://doi.org/10.1111/j.1467-9868.2004.02059.x) https://rss.onlinelibrary.wiley.com/doi/pdf/10.1111/j.1467-9868.2004.02059.x, <https://rss.onlinelibrary.wiley.com/doi/abs/10.1111/j.1467-9868.2004.02059.x>.

See Also

Other clustering algorithms: [GMMClustering\(](#page-39-1)), [HierarchicalClustering\(](#page-54-1)), [KMeansClustering\(](#page-59-1)), [PAMClustering\(](#page-69-1))

Examples

```
if (requireNamespace("dbscan", quietly = TRUE)) {
 # Data simulation
 set.seed(1)
 simul \le SimulateClustering(n = c(10, 10), pk = 50)
 plot(simul)
 # DBSCAN clustering
 myclust <- DBSCANClustering(
   xdata = simul$data,
   eps = seq(0, 2 * sqrt(ncol(simul$data) - 1), by = 0.1)\lambda# Weighted PAM clustering (using COSA)
 if (requireNamespace("rCOSA", quietly = TRUE)) {
   myclust <- DBSCANClustering(
     xdata = simul$data,
     eps = c(0.25, 0.5, 0.75),
     Lambda = c(0.2, 0.5))
 }
}
```


Ensemble *Ensemble model*

Description

Creates an ensemble predictive model from [VariableSelection](#page-117-1) outputs.

Usage

Ensemble(stability, xdata, ydata)

Arguments

Value

An object of class ensemble_model. A list with:

See Also

Other ensemble model functions: [EnsemblePredictions\(](#page-32-1))

Examples

```
# Linear regression
set.seed(1)
simul \le SimulateRegression(n = 100, pk = 50, family = "gaussian")
stab <- VariableSelection(xdata = simul$xdata, ydata = simul$ydata, family = "gaussian")
ensemble <- Ensemble(stability = stab, xdata = simul$xdata, ydata = simul$ydata)
# Logistic regression
set.seed(1)
simul <- SimulateRegression(n = 200, pk = 20, family = "binomial")
stab <- VariableSelection(xdata = simul$xdata, ydata = simul$ydata, family = "binomial")
ensemble <- Ensemble(stability = stab, xdata = simul$xdata, ydata = simul$ydata)
```
EnsemblePredictions *Predictions from ensemble model*

Description

Makes predictions using an ensemble model created from [VariableSelection](#page-117-1) outputs. For each observation in xdata, the predictions are calculated as the average predicted values obtained for that observation over the K models fitted in calibrated stability selection.

Usage

```
EnsemblePredictions(ensemble, xdata, ...)
```
Arguments

Value

A matrix of predictions computed from the observations in xdata.

See Also

[predict.variable_selection](#page-84-1)

Other ensemble model functions: [Ensemble\(](#page-31-1))

Examples

```
# Data simulation
set.seed(1)
simul \le SimulateRegression(n = 1000, pk = 50, family = "gaussian")
# Training/test split
ids \le Split(data = simul$ydata, tau = c(0.8, 0.2))
stab <- VariableSelection(
  xdata = simul$xdata[ids[[1]], ],
  ydata = simul$ydata[ids[[1]], ]
\lambda# Constructing the ensemble model
ensemble <- Ensemble(
  stability = stab,
  xdata = simul$xdata[ids[[1]], ],
  ydata = simul$ydata[ids[[1]], ]
)
# Making predictions
yhat <- EnsemblePredictions(
  ensemble = ensemble,
  xdata = simul$xdata[ids[[2]], ]
)
# Calculating Q-squared
cor(simul$ydata[ids[[2]], ], yhat)^2
```
ExplanatoryPerformance

Prediction performance in regression

Description

Calculates model performance for linear (measured by Q-squared), logistic (AUC) or Cox (Cstatistic) regression. This is done by (i) refitting the model on a training set including a proportion tau of the observations, and (ii) evaluating the performance on the remaining observations (test set). For more reliable results, the procedure can be repeated K times (default K=1).

ExplanatoryPerformance 35

Usage

```
ExplanatoryPerformance(
 xdata,
 ydata,
 new_xdata = NULL,
 new_ydata = NULL,
  stability = NULL,
  family = NULL,
  implementation = NULL,
 prediction = NULL,
 resampling = "subsampling",
 K = 1,tau = 0.8,
  seed = 1,
 n_thr = NULL,
 time = 1000,
 verbose = FALSE,
  ...
```

```
\mathcal{L}
```
Arguments

Details

For a fair evaluation of the prediction performance, the data is split into a training set (including a proportion tau of the observations) and test set (remaining observations). The regression model is fitted on the training set and applied on the test set. Performance metrics are computed in the test set by comparing predicted and observed outcomes.

For logistic regression, a Receiver Operating Characteristic (ROC) analysis is performed: the True and False Positive Rates (TPR and FPR), and Area Under the Curve (AUC) are computed for different thresholds in predicted probabilities.

For Cox regression, the Concordance Index (as implemented in [concordance](#page-0-0)) looking at survival probabilities up to a specific time is computed.

For linear regression, the squared correlation between predicted and observed outcome in the test set (Q-squared) is reported.

Value

A list with:

See Also

[VariableSelection](#page-117-1), [Refit](#page-87-1)

Other prediction performance functions: [Incremental\(](#page-56-1))
ExplanatoryPerformance 37

Examples

```
# Data simulation
set.seed(1)
simul <- SimulateRegression(
  n = 1000, pk = 20,
  family = "binomial", ev_{xy} = 0.8)
# Data split: selection, training and test set
ids <- Split(
  data = simul$ydata,
  family = "binomial",
  tau = c(0.4, 0.3, 0.3))
xselect <- simul$xdata[ids[[1]], ]
yselect <- simul$ydata[ids[[1]], ]
xtrain <- simul$xdata[ids[[2]], ]
ytrain <- simul$ydata[ids[[2]], ]
xtest <- simul$xdata[ids[[3]], ]
ytest <- simul$ydata[ids[[3]], ]
# Stability selection
stab <- VariableSelection(
 xdata = xselect,
 ydata = yselect,
  family = "binomial"
\lambda# Performances in test set of model refitted in training set
roc <- ExplanatoryPerformance(
  xdata = xtrain, ydata = ytrain,
  new_xdata = xtest, new_ydata = ytest,
  stability = stab
)
plot(roc)
roc$AUC
# Alternative with multiple training/test splits
roc <- ExplanatoryPerformance(
  xdata = rbind(xtrain, xtest),
  ydata = c(ytrain, ytest),
  stability = stab, K = 100\mathcal{L}plot(roc)
boxplot(roc$AUC)
# Partial Least Squares Discriminant Analysis
if (requireNamespace("sgPLS", quietly = TRUE)) {
  stab <- VariableSelection(
    xdata = xselect,
    ydata = yselect,
    implementation = SparsePLS,
```

```
family = "binomial"
 )
 # Defining wrapping functions for predictions from PLS-DA
 PLSDA <- function(xdata, ydata, family = "binomial") {
   model <- mixOmics::plsda(X = xdata, Y = as.factor(ydata), ncomp = 1)
   return(model)
 }
 PredictPLSDA <- function(xdata, model) {
   xdata <- xdata[, rownames(model$loadings$X), drop = FALSE]
   predicted <- predict(object = model, newdata = xdata)$predict[, 2, 1]
   return(predicted)
 }
 # Performances with custom models
 roc <- ExplanatoryPerformance(
   xdata = rbind(xtrain, xtest),
   ydata = c(ytrain, ytest),
   stability = stab, K = 100,
    implementation = PLSDA, prediction = PredictPLSDA
 )
 plot(roc)
}
```
FDP *False Discovery Proportion*

Description

Computes the False Discovery Proportion (upper-bound) as a ratio of the PFER (upper-bound) over the number of stably selected features. In stability selection, the FDP corresponds to the expected proportion of stably selected features that are not relevant to the outcome (i.e. proportion of False Positives among stably selected features).

Usage

FDP(selprop, PFER, pi)

Arguments

Value

The estimated upper-bound in FDP.

Folds 39

See Also

Other stability metric functions: [ConsensusScore\(](#page-28-0)), [PFER\(](#page-76-0)), [StabilityMetrics\(](#page-105-0)), [StabilityScore\(](#page-109-0))

Examples

Simulating set of selection proportions selprop \le round(runif(n = 20), digits = 2)

Computing the FDP with a threshold of 0.8 fdp <- FDP(PFER = 3, selprop = selprop, $pi = 0.8$)

Folds *Splitting observations into folds*

Description

Generates a list of n_folds non-overlapping sets of observation IDs (folds).

Usage

Folds(data, family = NULL, n_folds = 5)

Arguments

Details

For categorical outcomes (i.e. family argument is set to "binomial", "multinomial" or "cox"), the split is done such that the proportion of observations from each of the categories in each of the folds is representative of that of the full sample.

Value

A list of length n_folds with sets of non-overlapping observation IDs.

Examples

```
# Splitting into 5 folds
simul <- SimulateRegression()
ids <- Folds(data = simul$ydata)
lapply(ids, length)
# Balanced folds with respect to a binary variable
simul <- SimulateRegression(family = "binomial")
ids <- Folds(data = simul$ydata, family = "binomial")
lapply(ids, FUN = function(x) {
  table(simul$ydata[x, ])
})
```
GMMClustering *Model-based clustering*

Description

Runs clustering with Gaussian Mixture Models (GMM) using implementation from [Mclust](#page-0-0). This function is not using stability.

Usage

GMMClustering(xdata, nc = NULL, ...)

Arguments

Value

A list with:

See Also

Other clustering algorithms: [DBSCANClustering\(](#page-29-0)), [HierarchicalClustering\(](#page-54-0)), [KMeansClustering\(](#page-59-0)), [PAMClustering\(](#page-69-0))

Graph 41

Examples

```
# Data simulation
set.seed(1)
simul <- SimulateClustering(n = c(10, 10), pk = 50)
# Clustering using Gaussian Mixture Models
mygmm <- GMMClustering(xdata = simul$data, nc = seq_len(30))
```


Graph *Graph visualisation*

Description

Produces an [igraph](#page-0-0) object from an adjacency matrix.

Usage

```
Graph(
  adjacency,
  node_label = NULL,
 node_colour = NULL,
  node_shape = NULL,
  edge_colour = "grey60",
  label_colour = "grey20",
 mode = "undirected",
 weighted = FALSE,satellites = FALSE
\mathcal{L}
```
Arguments

Details

All functionalities implemented in [igraph](#page-0-0) can be used on the output. These include cosmetic changes for the visualisation, but also various tools for network analysis (including topological properties and community detection).

The R package [visNetwork](#page-0-0) offers interactive network visualisation tools. An [igraph](#page-0-0) object can easily be converted to a [visNetwork](#page-0-0) object (see example below).

For Cytoscape users, the [RCy3](#page-0-0) package can be used to open the network in Cytoscape.

Value

An igraph object.

See Also

[Adjacency](#page-110-0), [GraphicalModel](#page-45-0), [igraph manual,](https://igraph.org/r/) [visNetwork manual,](http://datastorm-open.github.io/visNetwork/) [Cytoscape](https://cytoscape.org)

Examples

```
## From adjacency matrix
```

```
# Un-weighted
adjacency <- SimulateAdjacency(pk = 20, topology = "scale-free")
plot(Graph(adjacency))
```

```
# Weighted
adjacency <- adjacency * runif(prod(dim(adjacency)))
adjacency <- adjacency + t(adjacency)
plot(Graph(adjacency, weighted = TRUE))
```

```
# Node colours and shapes
plot(Graph(adjacency, weighted = TRUE, node_shape = "star", node_colour = "red"))
```
From stability selection outputs

Graphical model

GraphComparison 43

```
set.seed(1)
simul <- SimulateGraphical(pk = 20)
stab <- GraphicalModel(xdata = simul$data)
plot(Graph(stab))
# Sparse PLS
if (requireNamespace("sgPLS", quietly = TRUE)) {
  set.seed(1)
  simul \le SimulateRegression(n = 50, pk = c(5, 5, 5), family = "gaussian")
  x <- simul$xdata
  y <- simul$ydata
  stab <- BiSelection(
    xdata = simul$xdata, ydata = simul$ydata,
    family = "gaussian", ncomp = 3,
   LambdaX = seq\_len(ncol(x) - 1),
   implementation = SparsePLS
  )
  plot(Graph(stab))
}
## Tools from other packages
# Applying some igraph functionalities
adjacency <- SimulateAdjacency(pk = 20, topology = "scale-free")
mygraph <- Graph(adjacency)
igraph::degree(mygraph)
igraph::betweenness(mygraph)
igraph::shortest_paths(mygraph, from = 1, to = 2)
igraph::walktrap.community(mygraph)
# Interactive view using visNetwork
if (requireNamespace("visNetwork", quietly = TRUE)) {
  vgraph <- mygraph
  igraph::V(vgraph)$shape <- rep("dot", length(igraph::V(vgraph)))
  v <- visNetwork::visIgraph(vgraph)
  mylayout <- as.matrix(v$x$nodes[, c("x", "y")])
  mylayout[, 2] <- -mylayout[, 2]
  plot(mygraph, layout = mylayout)
}
# Opening in Cytoscape using RCy3
if (requireNamespace("RCy3", quietly = TRUE)) {
  # Make sure that Cytoscape is open before running the following line
  # RCy3::createNetworkFromIgraph(mygraph)
}
```
Description

Generates an [igraph](#page-0-0) object representing the common and graph-specific edges.

Usage

```
GraphComparison(
 graph1,
 graph2,
 col = c("tomato", "forestgreen", "navy"),
 lty = c(2, 3, 1),node_colour = NULL,
 show_labels = TRUE,
  ...
\mathcal{L}
```
Arguments

Value

An igraph object.

See Also

[SelectionPerformanceGraph](#page-95-0)

Examples

```
# Data simulation
set.seed(1)
simul1 <- SimulateGraphical(pk = 30)
set.seed(2)
simul2 <- SimulateGraphical(pk = 30)
```
GraphicalAlgo 45

```
# Edge-wise comparison of the two graphs
mygraph <- GraphComparison(
 graph1 = simu11,graph2 = simu12)
plot(mygraph, layout = igraph::layout_with_kk(mygraph))
```
GraphicalAlgo *Graphical model algorithm*

Description

Runs the algorithm specified in the argument implementation and returns the estimated adjacency matrix. This function is not using stability.

Usage

```
GraphicalAlgo(
  xdata,
 pk = NULL,Lambda,
  Sequential_template = NULL,
  scale = TRUE,
  implementation = PenalisedGraphical,
  start = "cold",...
\mathcal{L}
```
Arguments

currently being calibrated and FALSE for other blocks). Other approaches with joint calibration of the blocks are allowed (all entries are set to TRUE).

Details

The use of the procedure from Equation (4) or (5) is controlled by the argument "Sequential_template".

Value

An array with binary and symmetric adjacency matrices along the third dimension.

See Also

[GraphicalModel](#page-45-0), [PenalisedGraphical](#page-70-0) Other wrapping functions: [SelectionAlgo\(](#page-92-0))

Examples

```
# Data simulation
set.seed(1)
simul <- SimulateGraphical()
# Running graphical LASSO
myglasso <- GraphicalAlgo(
  xdata = simul$data,
  Lambda = cbind(c(0.1, 0.2)))
```
GraphicalModel *Stability selection graphical model*

Description

Performs stability selection for graphical models. The underlying graphical model (e.g. graphical LASSO) is run with different combinations of parameters controlling the sparsity (e.g. penalty parameter) and thresholds in selection proportions. These two hyper-parameters are jointly calibrated by maximisation of the stability score.

GraphicalModel 47

Usage

```
GraphicalModel(
  xdata,
  pk = NULL,Lambda = NULL,
  lambda_other_blocks = 0.1,
 pi_list = seq(0.01, 0.99, by = 0.01),
 K = 100,
  tau = 0.5,
  seed = 1,
  n_{cat} = NULL,implementation = PenalisedGraphical,
  start = "warm",scale = TRUE,resampling = "subsampling",
  cpss = FALSE,PFER_method = "MB",
 PFER_thr = Inf,
  FDP_{thr} = Inf,Lambda_cardinal = 50,
  lambda_max = NULL,
  lambda_path_factor = 0.001,
  max\_density = 0.5,
  optimisation = c("grid_search", "nloptr"),
  n\_cores = 1,output_data = FALSE,
  verbose = TRUE,
 beep = NULL,...
\mathcal{L}
```
Arguments

Details

In stability selection, a feature selection algorithm is fitted on K subsamples (or bootstrap samples) of the data with different parameters controlling the sparsity (Lambda). For a given (set of) sparsity parameter(s), the proportion out of the K models in which each feature is selected is calculated. Features with selection proportions above a threshold pi are considered stably selected. The stability selection model is controlled by the sparsity parameter(s) for the underlying algorithm, and the threshold in selection proportion:

 $V_{\lambda,\pi} = \{j : p_{\lambda}(j) \geq \pi\}$

These parameters can be calibrated by maximisation of a stability score (see [ConsensusScore](#page-28-0) if n_cat=NULL or [StabilityScore](#page-109-0) otherwise) calculated under the null hypothesis of equiprobability of selection.

It is strongly recommended to examine the calibration plot carefully to check that the grids of parameters Lambda and pi_list do not restrict the calibration to a region that would not include the global maximum (see [CalibrationPlot](#page-15-0)). In particular, the grid Lambda may need to be extended when the maximum stability is observed on the left or right edges of the calibration heatmap. In some instances, multiple peaks of stability score can be observed. Simulation studies suggest that the peak corresponding to the largest number of selected features tend to give better selection performances. This is not necessarily the highest peak (which is automatically retained by the functions in this package). The user can decide to manually choose another peak.

To control the expected number of False Positives (Per Family Error Rate) in the results, a threshold PFER_thr can be specified. The optimisation problem is then constrained to sets of parameters that generate models with an upper-bound in PFER below PFER_thr (see Meinshausen and Bühlmann (2010) and Shah and Samworth (2013)).

Possible resampling procedures include defining (i) K subsamples of a proportion tau of the observations, (ii) K bootstrap samples with the full sample size (obtained with replacement), and (iii) K/2 splits of the data in half for complementary pair stability selection (see arguments resampling and cpss). In complementary pair stability selection, a feature is considered selected at a given resampling iteration if it is selected in the two complementary subsamples.

To ensure reproducibility of the results, the starting number of the random number generator is set to seed.

For parallelisation, stability selection with different sets of parameters can be run on n_cores cores. Using n_cores > 1 creates a [multisession](#page-0-0). Alternatively, the function can be run manually with different seeds and all other parameters equal. The results can then be combined using [Combine](#page-26-0).

The generated network can be converted into [igraph](#page-0-0) object using [Graph](#page-40-0). The R package [visNetwork](#page-0-0) can be used for interactive network visualisation (see examples in [Graph](#page-40-0)).

Value

An object of class graphical_model. A list with:

The rows of S, Lambda, Q, Q_s, P, PFER, FDP, S_2d, PFER_2d and FDP_2d, and indices along the third dimension of selprop are ordered in the same way and correspond to parameter values stored in Lambda. For multi-block inference, the columns of S, Lambda, Q, Q_s, P, PFER and FDP, and indices along the third dimension of S_2d correspond to the different blocks.

References

Bodinier B, Filippi S, Nøst TH, Chiquet J, Chadeau-Hyam M (2023). "Automated calibration for stability selection in penalised regression and graphical models." *Journal of the Royal Statistical Society Series C: Applied Statistics*, qlad058. ISSN 0035-9254, [doi:10.1093/jrsssc/qlad058,](https://doi.org/10.1093/jrsssc/qlad058) https://academic.oup.com/jrsssc/advance-article-pdf/doi/10.1093/jrsssc/qlad058/50878777/qlad058.pdf.

Shah RD, Samworth RJ (2013). "Variable selection with error control: another look at stability selection." *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 75(1), 55- 80. [doi:10.1111/j.14679868.2011.01034.x.](https://doi.org/10.1111/j.1467-9868.2011.01034.x)

Meinshausen N, Bühlmann P (2010). "Stability selection." *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 72(4), 417-473. [doi:10.1111/j.14679868.2010.00740.x.](https://doi.org/10.1111/j.1467-9868.2010.00740.x)

Friedman J, Hastie T, Tibshirani R (2008). "Sparse inverse covariance estimation with the graphical lasso." *Biostatistics*, 9(3), 432–441.

See Also

[PenalisedGraphical](#page-70-0), [GraphicalAlgo](#page-44-0), [LambdaGridGraphical](#page-60-0), [Resample](#page-90-0), [StabilityScore](#page-109-0) [Graph](#page-40-0), [Adjacency](#page-110-0),

Other stability functions: [BiSelection\(](#page-7-0)), [Clustering\(](#page-19-0)), [StructuralModel\(](#page-112-0)), [VariableSelection\(](#page-117-0))

Examples

```
oldpar <- par(no.readonly = TRUE)
par(max = rep(7, 4))
```
Single-block stability selection

```
# Data simulation
set.seed(1)
simul \le SimulateGraphical(n = 100, pk = 20, nu_within = 0.1)
```

```
# Stability selection
stab <- GraphicalModel(xdata = simul$data)
print(stab)
```
Calibration heatmap CalibrationPlot(stab)

```
# Visualisation of the results
summary(stab)
plot(stab)
# Extraction of adjacency matrix or igraph object
Adjacency(stab)
Graph(stab)
## Multi-block stability selection
# Data simulation
set.seed(1)
simul <- SimulateGraphical(pk = c(10, 10))
# Stability selection
stab <- GraphicalModel(xdata = simul$data, pk = c(10, 10), Lambda_cardinal = 10)
print(stab)
# Calibration heatmap
# par(mfrow = c(1, 3))
CalibrationPlot(stab) # Producing three plots
# Visualisation of the results
summary(stab)
plot(stab)
# Multi-parameter stability selection (not recommended)
Lambda <- matrix(c(0.8, 0.6, 0.3, 0.5, 0.4, 0.3, 0.7, 0.5, 0.1), ncol = 3)
stab <- GraphicalModel(
 xdata = simul$data, pk = c(10, 10),Lambda = Lambda, lambda_other_blocks = NULL
\mathcal{L}stab$Lambda
## Example with user-defined function: shrinkage estimation and selection
# Data simulation
set.seed(1)
simul \le SimulateGraphical(n = 100, pk = 20, nu_within = 0.1)
if (requireNamespace("corpcor", quietly = TRUE)) {
  # Writing user-defined algorithm in a portable function
  ShrinkageSelection <- function(xdata, Lambda, ...) {
    mypcor <- corpcor::pcor.shrink(xdata, verbose = FALSE)
    adjacency <- array(NA, dim = c(nrow(mypcor), ncol(mypcor), nrow(Lambda)))
    for (k in seq_len(nrow(Lambda))) {
      A \leftarrow ifelse(abs(mypcor) >= Lambda[k, 1], yes = 1, no = 0)
      diag(A) <- 0
      adjacency[, , k] <- A
    }
```
GroupPLS 53

```
return(list(adjacency = adjacency))
 }
 # Running the algorithm without stability
 myglasso <- GraphicalAlgo(
   xdata = simul$data,
   Lambda = matrix(c(0.05, 0.1), ncol = 1), implementation = ShrinkageSelection
 )
 # Stability selection using shrinkage estimation and selection
 stab <- GraphicalModel(
   xdata = simul$data, Lambda = matrix(c(0.01, 0.05, 0.1), ncol = 1),implementation = ShrinkageSelection
 \lambdaCalibrationPlot(stab)
 stable_adjacency <- Adjacency(stab)
}
par(oldpar)
```
GroupPLS *Group Partial Least Squares*

Description

Runs a group Partial Least Squares model using implementation from [sgPLS-package](#page-0-0). This function is not using stability.

Usage

```
GroupPLS(
  xdata,
  ydata,
  family = "gaussian",
  group_x,
  group_y = NULL,Lambda,
  keepX_previous = NULL,
  keepY = NULL,
  ncomp = 1,
  scale = TRUE,
  ...
)
```
Arguments

xdata matrix of predictors with observations as rows and variables as columns.

Value

A list with:

References

Liquet B, de Micheaux PL, Hejblum BP, Thiébaut R (2016). "Group and sparse group partial least square approaches applied in genomics context." *Bioinformatics*, 32(1), 35-42. ISSN 1367-4803, [doi:10.1093/bioinformatics/btv535.](https://doi.org/10.1093/bioinformatics/btv535)

See Also

[VariableSelection](#page-117-0), [BiSelection](#page-7-0)

Other penalised dimensionality reduction functions: [SparseGroupPLS\(](#page-98-0)), [SparsePCA\(](#page-100-0)), [SparsePLS\(](#page-102-0))

HierarchicalClustering 55

Examples

```
if (requireNamespace("sgPLS", quietly = TRUE)) {
 ## Group PLS
 # Data simulation
 set.seed(1)
 simul \le SimulateRegression(n = 100, pk = 50, q = 3, family = "gaussian")
 x <- simul$xdata
 y <- simul$ydata
 # Running gPLS with 1 group and sparsity of 0.5
 mypls <- GroupPLS(
   xdata = x, ydata = y, Lambda = 1, family = "gaussian",group_x = c(10, 15, 25),\lambda# Running gPLS with groups on outcomes
 mypls <- GroupPLS(
   xdata = x, ydata = y, Lambda = 1, family = "gaussian",group_x = c(10, 15, 25),
   group_y = c(2, 1), keepY = 1
 )
}
```
HierarchicalClustering

(Weighted) hierarchical clustering

Description

Runs hierarchical clustering using implementation from [hclust](#page-0-0). If Lambda is provided, clustering is applied on the weighted distance matrix calculated using the [cosa2](#page-0-0) algorithm. Otherwise, distances are calculated using [dist](#page-0-0). This function is not using stability.

Usage

```
HierarchicalClustering(
  xdata,
  nc = NULL,
 Lambda = NULL,
  distance = "euclidean",
  linkage = "complete",
  ...
```
)

Arguments

xdata data matrix with observations as rows and variables as columns.

Value

A list with:

References

Kampert MM, Meulman JJ, Friedman JH (2017). "rCOSA: A Software Package for Clustering Objects on Subsets of Attributes." *Journal of Classification*, 34(3), 514–547. [doi:10.1007/s00357-](https://doi.org/10.1007/s00357-017-9240-z) [0179240z.](https://doi.org/10.1007/s00357-017-9240-z)

Friedman JH, Meulman JJ (2004). "Clustering objects on subsets of attributes (with discussion)." *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 66(4), 815-849. [doi:10.1](https://doi.org/10.1111/j.1467-9868.2004.02059.x)111/ [j.14679868.2004.02059.x,](https://doi.org/10.1111/j.1467-9868.2004.02059.x) https://rss.onlinelibrary.wiley.com/doi/pdf/10.1111/j.1467-9868.2004.02059.x, <https://rss.onlinelibrary.wiley.com/doi/abs/10.1111/j.1467-9868.2004.02059.x>.

See Also

Other clustering algorithms: [DBSCANClustering\(](#page-29-0)), [GMMClustering\(](#page-39-0)), [KMeansClustering\(](#page-59-0)), [PAMClustering\(](#page-69-0))

Examples

```
# Data simulation
set.seed(1)
simul \le SimulateClustering(n = c(10, 10), pk = 50)
# Hierarchical clustering
myhclust <- HierarchicalClustering(
```
Incremental 57

```
xdata = simul$data,
  nc = seq\_len(20))
# Weighted Hierarchical clustering (using COSA)
if (requireNamespace("rCOSA", quietly = TRUE)) {
  myhclust <- HierarchicalClustering(
    xdata = simul$data,
   weighted = TRUE,
   nc = seq\_len(20),
   Lambda = c(0.2, 0.5))
}
```
Incremental *Incremental prediction performance in regression*

Description

Computes the prediction performance of regression models where predictors are sequentially added by order of decreasing selection proportion. This function can be used to evaluate the marginal contribution of each of the selected predictors over and above more stable predictors. Performances are evaluated as in [ExplanatoryPerformance](#page-33-0).

Usage

```
Incremental(
  xdata,
  ydata,
  new_xdata = NULL,
  new_ydata = NULL,
  stability = NULL,
  family = NULL,
  implementation = NULL,
  prediction = NULL,
  resampling = "subsampling",
  n_predictors = NULL,
 K = 100,
  tau = 0.8,
  seed = 1,
  n_{thr} = NULL,
  time = 1000,
  verbose = TRUE,
  ...
)
```
Arguments

Value

An object of class incremental.

For logistic regression, a list with:

For Cox regression, a list with:

For linear regression, a list with:

See Also

[VariableSelection](#page-117-0), [Refit](#page-87-0)

Other prediction performance functions: [ExplanatoryPerformance\(](#page-33-0))

Examples

```
# Data simulation
set.seed(1)
simul <- SimulateRegression(
  n = 1000, pk = 20,
  family = "binomial", ev_{xy} = 0.8\overline{)}# Data split: selection, training and test set
ids <- Split(
 data = simul$ydata,
 family = "binomial",
  tau = c(0.4, 0.3, 0.3)
```

```
)
xselect <- simul$xdata[ids[[1]], ]
yselect <- simul$ydata[ids[[1]], ]
xtrain <- simul$xdata[ids[[2]], ]
ytrain <- simul$ydata[ids[[2]], ]
xtest <- simul$xdata[ids[[3]], ]
ytest <- simul$ydata[ids[[3]], ]
# Stability selection
stab <- VariableSelection(
  xdata = xselect,
  ydata = yselect,
  family = "binomial"
\mathcal{L}# Performances in test set of model refitted in training set
incr <- Incremental(
  xdata = xtrain, ydata = ytrain,
  new_xdata = xtest, new_ydata = ytest,
  stability = stab, n_predictors = 10
)
plot(incr)
# Alternative with multiple training/test splits
incr <- Incremental(
  xdata = rbind(xtrain, xtest),
  ydata = c(ytrain, ytest),
  stability = stab, K = 10, n_predictors = 10
)
plot(incr)
```
KMeansClustering *(Sparse) K-means clustering*

Description

Runs k-means clustering using implementation from [kmeans](#page-0-0). This function is not using stability.

Usage

```
KMeansClustering(xdata, nc = NULL, Lambda = NULL, ...)
```
Arguments

A list with:

Value

comembership an array of binary and symmetric co-membership matrices. weights a matrix of median weights by feature.

References

Witten DM, Tibshirani R (2010). "A Framework for Feature Selection in Clustering." *Journal of the American Statistical Association*, 105(490), 713-726. [doi:10.1198/jasa.2010.tm09415,](https://doi.org/10.1198/jasa.2010.tm09415) PMID: 20811510.

See Also

Other clustering algorithms: [DBSCANClustering\(](#page-29-0)), [GMMClustering\(](#page-39-0)), [HierarchicalClustering\(](#page-54-0)), [PAMClustering\(](#page-69-0))

Examples

```
# Data simulation
set.seed(1)
simul \le SimulateClustering(n = c(10, 10), pk = 50)
# K means clustering
mykmeans <- KMeansClustering(xdata = simul$data, nc = seq_len(20))
# Sparse K means clustering
if (requireNamespace("sparcl", quietly = TRUE)) {
 mykmeans <- KMeansClustering(
   xdata = simul$data, nc = seq_len(20),
   Lambda = c(2, 5))
}
```
LambdaGridGraphical *Grid of penalty parameters (graphical model)*

Description

Generates a relevant grid of penalty parameter values for penalised graphical models.

Usage

```
LambdaGridGraphical(
  xdata,
  pk = NULL,
  lambda_other_blocks = 0.1,
  K = 100,
  tau = 0.5,
  n_{cat} = 3,
  implementation = PenalisedGraphical,
  start = "cold",scale = TRUE,
  resampling = "subsampling",
  PFER_method = "MB",
  PFER_thr = Inf,
  FDP_{thr} = Inf,Lambda_cardinal = 50,
  lambda_max = NULL,lambda_path_factor = 0.001,
  max\_density = 0.5,
  ...
)
```
Arguments

Value

A matrix of lambda values with length(pk) columns and Lambda_cardinal rows.

See Also

Other lambda grid functions: [LambdaGridRegression\(](#page-63-0)), [LambdaSequence\(](#page-65-0))

Examples

Single-block simulation

```
set.seed(1)
simul <- SimulateGraphical()
# Generating grid of 10 values
Lambda <- LambdaGridGraphical(xdata = simul$data, Lambda_cardinal = 10)
# Ensuring PFER < 5
Lambda <- LambdaGridGraphical(xdata = simul$data, Lambda_cardinal = 10, PFER_thr = 5)
# Multi-block simulation
set.seed(1)
simul <- SimulateGraphical(pk = c(10, 10))
# Multi-block grid
Lambda <- LambdaGridGraphical(xdata = simul$data, pk = c(10, 10), Lambda_cardinal = 10)
# Denser neighbouring blocks
Lambda <- LambdaGridGraphical(
  xdata = simul$data, pk = c(10, 10),Lambda_cardinal = 10, lambda_other_blocks = 0\mathcal{L}# Using different neighbour penalties
Lambda <- LambdaGridGraphical(
  xdata = simul$data, pk = c(10, 10),Lambda_cardinal = 10, lambda_other_blocks = c(0.1, 0, 0.1))
stab <- GraphicalModel(
  xdata = simul$data, pk = c(10, 10),Lambda = Lambda, lambda_other_blocks = c(0.1, 0, 0.1)
\lambdastab$Lambda
# Visiting from empty to full graphs with max_density=1
Lambda <- LambdaGridGraphical(
  xdata = simul$data, pk = c(10, 10),Lambda_cardinal = 10, max_density = 1
)
bigblocks <- BlockMatrix(pk = c(10, 10))
bigblocks_vect <- bigblocks[upper.tri(bigblocks)]
N_blocks <- unname(table(bigblocks_vect))
N_blocks # max number of edges per block
stab <- GraphicalModel(xdata = simul$data, pk = c(10, 10), Lambda = Lambda)
apply(stab$Q, 2, max, na.rm = TRUE) # max average number of edges from underlying algo
```
LambdaGridRegression *Grid of penalty parameters (regression model)*

Description

Generates a relevant grid of penalty parameter values for penalised regression using the implementation in [glmnet](#page-0-0).

Usage

```
LambdaGridRegression(
 xdata,
 ydata,
 tau = 0.5,
  seed = 1,
  family = "gaussian",
 resampling = "subsampling",
 Lambda_cardinal = 100,
 check_input = TRUE,
  ...
)
```
Arguments

Value

A matrix of lambda values with one column and as many rows as indicated in Lambda_cardinal.

See Also

Other lambda grid functions: [LambdaGridGraphical\(](#page-60-0)), [LambdaSequence\(](#page-65-0))

Examples

```
# Data simulation
set.seed(1)
simul \le SimulateRegression(n = 100, pk = 50, family = "gaussian") # simulated data
# Lambda grid for linear regression
Lambda <- LambdaGridRegression(
  xdata = simul$xdata, ydata = simul$ydata,
  family = "gaussian", Lambda_cardinal = 20
\lambda# Grid can be used in VariableSelection()
stab <- VariableSelection(
  xdata = simul$xdata, ydata = simul$ydata,
  family = "gaussian", Lambda = Lambda
)
print(SelectedVariables(stab))
```
LambdaSequence *Sequence of penalty parameters*

Description

Generates a sequence of penalty parameters from extreme values and the required number of elements. The sequence is defined on the log-scale.

Usage

LambdaSequence(lmax, lmin, cardinal = 100)

Arguments

Value

A vector with values between "lmin" and "lmax" and as many values as indicated by "cardinal".

See Also

Other lambda grid functions: [LambdaGridGraphical\(](#page-60-0)), [LambdaGridRegression\(](#page-63-0))

LinearSystemMatrix 67

Examples

```
# Grid from extreme values
mygrid \le LambdaSequence(lmax = 0.7, lmin = 0.001, cardinal = 10)
```
LinearSystemMatrix *Matrix from linear system outputs*

Description

Returns a matrix from output of [PenalisedLinearSystem](#page-72-0).

Usage

```
LinearSystemMatrix(vect, adjacency)
```
Arguments

Value

An asymmetric matrix.

See Also

[PenalisedLinearSystem](#page-72-0)

OpenMxMatrix *Matrix from OpenMx outputs*

Description

Returns a matrix from output of [mxPenaltySearch](#page-0-0).

Usage

```
OpenMxMatrix(vect, adjacency, residual_covariance = NULL)
```
Arguments

Value

An asymmetric matrix.

See Also

[PenalisedOpenMx](#page-72-1), [OpenMxModel](#page-67-0)

OpenMxModel *Writing OpenMx model (matrix specification)*

Description

Returns matrix specification for use in $m \times \text{Model}$ from (i) the adjacency matrix of a Directed Acyclic Graph (asymmetric matrix A in Reticular Action Model notation), and (ii) a binary matrix encoding nonzero entries in the residual covariance matrix (symmetric matrix S in Reticular Action Model notation).

Usage

```
OpenMxModel(adjacency, residual_covariance = NULL, manifest = NULL)
```
Arguments

Value

A list of RAM matrices that can be used in [mxRun](#page-0-0).

OpenMxModel 69

See Also

[PenalisedOpenMx](#page-72-1), [OpenMxMatrix](#page-66-0)

Examples

```
if (requireNamespace("OpenMx", quietly = TRUE)) {
 # Definition of simulated effects
 pk \leftarrow c(3, 2, 3)dag <- LayeredDAG(layers = pk)
 theta <- dag
 theta[2, 4] <- 0
 theta[3, 7] <- 0
 theta[4, 7] <- 0
 # Data simulation
 set.seed(1)
 simul \le SimulateStructural(n = 500, v_between = 1, theta = theta, pk = pk)
 # Writing RAM matrices for mxModel
 ram_matrices <- OpenMxModel(adjacency = dag)
 # Running unpenalised model
 unpenalised <- OpenMx::mxRun(OpenMx::mxModel(
    "Model",
   OpenMx::mxData(simul$data, type = "raw"),
   ram_matrices$Amat,
   ram_matrices$Smat,
   ram_matrices$Fmat,
   ram_matrices$Mmat,
   OpenMx::mxExpectationRAM("A", "S", "F", "M", dimnames = colnames(dag)),
   OpenMx::mxFitFunctionML()
 ), silent = TRUE, suppressWarnings = TRUE)
 unpenalised$A$values
 # Incorporating latent variables
 ram_matrices <- OpenMxModel(
   adjacency = dag,
   manifest = paste@("x", seq_length(7)))
 ram_matrices$Fmat$values
 # Running unpenalised model
 unpenalised <- OpenMx::mxRun(OpenMx::mxModel(
    "Model",
   OpenMx::mxData(simul$data[, seq_len(7)], type = "raw"),
   ram_matrices$Amat,
   ram_matrices$Smat,
   ram_matrices$Fmat,
   ram_matrices$Mmat,
   OpenMx::mxExpectationRAM("A", "S", "F", "M", dimnames = colnames(dag)),
   OpenMx::mxFitFunctionML()
 ), silent = TRUE, suppressWarnings = TRUE)
```

```
unpenalised$A$values
}
```


Description

Runs Partitioning Around Medoids (PAM) clustering using implementation from [pam](#page-0-0). This is also known as the k-medoids algorithm. If Lambda is provided, clustering is applied on the weighted distance matrix calculated using the COSA algorithm as implemented in [cosa2](#page-0-0). Otherwise, distances are calculated using [dist](#page-0-0). This function is not using stability.

Usage

```
PAMClustering(xdata, nc = NULL, Lambda = NULL, distance = "euclidean", ...)
```
Arguments

Value

A list with:

References

Kampert MM, Meulman JJ, Friedman JH (2017). "rCOSA: A Software Package for Clustering Objects on Subsets of Attributes." *Journal of Classification*, 34(3), 514–547. [doi:10.1007/s00357-](https://doi.org/10.1007/s00357-017-9240-z) [0179240z.](https://doi.org/10.1007/s00357-017-9240-z)

Friedman JH, Meulman JJ (2004). "Clustering objects on subsets of attributes (with discussion)." *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 66(4), 815-849. [doi:10.1](https://doi.org/10.1111/j.1467-9868.2004.02059.x)111/ [j.14679868.2004.02059.x,](https://doi.org/10.1111/j.1467-9868.2004.02059.x) https://rss.onlinelibrary.wiley.com/doi/pdf/10.1111/j.1467-9868.2004.02059.x, <https://rss.onlinelibrary.wiley.com/doi/abs/10.1111/j.1467-9868.2004.02059.x>.

PenalisedGraphical 71

See Also

Other clustering algorithms: [DBSCANClustering\(](#page-29-0)), [GMMClustering\(](#page-39-0)), [HierarchicalClustering\(](#page-54-0)), [KMeansClustering\(](#page-59-0))

Examples

```
if (requireNamespace("cluster", quietly = TRUE)) {
 # Data simulation
 set.seed(1)
 simul \le SimulateClustering(n = c(10, 10), pk = 50)
 # PAM clustering
 myclust <- PAMClustering(
   xdata = simul$data,
   nc = seq\_len(20)\lambda# Weighted PAM clustering (using COSA)
 if (requireNamespace("rCOSA", quietly = TRUE)) {
   myclust <- PAMClustering(
      xdata = simul$data,
      nc = seq\_len(20),
     Lambda = c(0.2, 0.5))
 }
}
```
PenalisedGraphical *Graphical LASSO*

Description

Runs the graphical LASSO algorithm for estimation of a Gaussian Graphical Model (GGM). This function is not using stability.

Usage

```
PenalisedGraphical(
  xdata,
  pk = NULL,Lambda,
  Sequential_template = NULL,
  scale = TRUE,
  start = "cold".
  output_omega = FALSE,
  ...
)
```
Arguments

Details

The use of the procedure from Equation (4) or (5) is controlled by the argument "Sequential_template".

Value

An array with binary and symmetric adjacency matrices along the third dimension.

References

Friedman J, Hastie T, Tibshirani R (2008). "Sparse inverse covariance estimation with the graphical lasso." *Biostatistics*, 9(3), 432–441.

See Also

[GraphicalModel](#page-45-0)

Other underlying algorithm functions: [CART\(](#page-17-0)), [ClusteringAlgo\(](#page-23-0)), [PenalisedOpenMx\(](#page-72-1)), [PenalisedRegression\(](#page-74-0))
PenalisedOpenMx 73

Examples

```
# Data simulation
set.seed(1)
simul <- SimulateGraphical()
# Running graphical LASSO
myglasso <- PenalisedGraphical(
  xdata = simul$data,
  Lambda = matrix(c(0.1, 0.2), ncol = 1))
# Returning estimated precision matrix
myglasso <- PenalisedGraphical(
  xdata = simul$data,
 Lambda = matrix(c(0.1, 0.2), ncol = 1),
  output_omega = TRUE
\lambda
```
PenalisedOpenMx *Penalised Structural Equation Model*

Description

Runs penalised Structural Equation Modelling using implementations from [OpenMx](#page-0-0) functions (for [PenalisedOpenMx](#page-72-0)), or using series of penalised regressions with [glmnet](#page-0-0) (for [PenalisedLinearSystem](#page-72-1)). The function [PenalisedLinearSystem](#page-72-1) does not accommodate latent variables. These functions are not using stability.

Usage

```
PenalisedOpenMx(
  xdata,
  adjacency,
  penalised = NULL,
  residual_covariance = NULL,
  Lambda,
  ...
\mathcal{L}
```
PenalisedLinearSystem(xdata, adjacency, penalised = NULL, Lambda = NULL, ...)

Value

References

Jacobucci R, Grimm KJ, McArdle JJ (2016). "Regularized structural equation modeling." *Structural equation modeling: a multidisciplinary journal*, 23(4), 555–566. [doi:10.1080/10705511.2016.1154793.](https://doi.org/10.1080/10705511.2016.1154793)

See Also

[SelectionAlgo](#page-92-0), [VariableSelection](#page-117-0), [OpenMxMatrix](#page-66-0), [LinearSystemMatrix](#page-66-1)

Other underlying algorithm functions: [CART\(](#page-17-0)), [ClusteringAlgo\(](#page-23-0)), [PenalisedGraphical\(](#page-70-0)), [PenalisedRegression\(](#page-74-0))

```
# Data simulation
pk <- c(3, 2, 3)
dag <- LayeredDAG(layers = pk)
theta <- dag
theta[2, 4] <- 0
set.seed(1)
simul \le SimulateStructural(theta = theta, pk = pk, output_matrices = TRUE)
# Running regularised SEM (OpenMx)
if (requireNamespace("OpenMx", quietly = TRUE)) {
  mysem <- PenalisedOpenMx(
   xdata = simul$data, adjacency = dag,
   Lambda = seq(1, 10, 1))
  OpenMxMatrix(vect = mysem$selected[3, ], adjacency = dag)
}
# Running regularised SEM (glmnet)
mysem <- PenalisedLinearSystem(
```

```
xdata = simul$data, adjacency = dag
)
LinearSystemMatrix(vect = mysem$selected[20, ], adjacency = dag)
```
PenalisedRegression *Penalised regression*

Description

Runs penalised regression using implementation from [glmnet](#page-0-0). This function is not using stability.

Usage

```
PenalisedRegression(
  xdata,
  ydata,
  Lambda = NULL,
  family,
  penalisation = c("classic", "randomised", "adaptive"),
  gamma = NULL,
  ...
\mathcal{L}
```


Value

A list with:

References

Zou H (2006). "The adaptive lasso and its oracle properties." *Journal of the American statistical association*, 101(476), 1418–1429.

Tibshirani R (1996). "Regression Shrinkage and Selection via the Lasso." *Journal of the Royal Statistical Society. Series B (Methodological)*, 58(1), 267–288. ISSN 00359246, [http://www.](http://www.jstor.org/stable/2346178) [jstor.org/stable/2346178](http://www.jstor.org/stable/2346178).

See Also

[SelectionAlgo](#page-92-0), [VariableSelection](#page-117-0)

Other underlying algorithm functions: [CART\(](#page-17-0)), [ClusteringAlgo\(](#page-23-0)), [PenalisedGraphical\(](#page-70-0)), [PenalisedOpenMx\(](#page-72-0))

```
# Data simulation
set.seed(1)
simul <- SimulateRegression(pk = 50)
# Running the LASSO
mylasso <- PenalisedRegression(
  xdata = simul$xdata, ydata = simul$ydata,
  Lambda = c(0.1, 0.2), family = "gaussian"
)
# Using glmnet arguments
mylasso <- PenalisedRegression(
  xdata = simul$xdata, ydata = simul$ydata,
  Lambda = c(0.1), family = "gaussian",
  penalty.factor = c(rep(\theta, 1\theta), rep(1, 4\theta))\lambdamylasso$beta_full
```
Description

Computes the Per Family Error Rate upper-bound of a stability selection model using the methods proposed by Meinshausen and Bühlmann (2010) or Shah and Samworth (2013). In stability selection, the PFER corresponds to the expected number of stably selected features that are not relevant to the outcome (i.e. False Positives).

Usage

PFER(q, pi, N, K, PFER_method = "MB")

Arguments

Value

The estimated upper-bound in PFER.

References

Meinshausen N, Bühlmann P (2010). "Stability selection." *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 72(4), 417-473. [doi:10.1111/j.14679868.2010.00740.x.](https://doi.org/10.1111/j.1467-9868.2010.00740.x)

Shah RD, Samworth RJ (2013). "Variable selection with error control: another look at stability selection." *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 75(1), 55- 80. [doi:10.1111/j.14679868.2011.01034.x.](https://doi.org/10.1111/j.1467-9868.2011.01034.x)

See Also

Other stability metric functions: [ConsensusScore\(](#page-28-0)), [FDP\(](#page-37-0)), [StabilityMetrics\(](#page-105-0)), [StabilityScore\(](#page-109-0))

Description

Creates a heatmap of the (calibrated) consensus matrix. See examples in [Clustering](#page-19-0).

Usage

```
## S3 method for class 'clustering'
plot(
 x,
 linkage = "complete",
 argmax_id = NULL,theta = NULL,
  theta_star = NULL,
  col = c("ivory", "navajowhite", "tomato", "darkred"),
 lines = TRUE,
 col.lines = c("blue"),
 lwd.lines = 2,
 tick = TRUE,
 axes = TRUE,col.axis = NULL,
 cex. axis = 1,xlas = 2,
 ylas = 2,
 bty = "n",...
)
```


plot.incremental 79

Value

A heatmap.

plot.incremental *Plot of incremental performance*

Description

Represents prediction performances upon sequential inclusion of the predictors in a logistic or Cox regression model as produced by [Incremental](#page-56-0). The median and quantiles of the performance metric are reported. See examples in [Incremental](#page-56-0).

Usage

```
## S3 method for class 'incremental'
plot(
 x,
  quantiles = c(0.05, 0.95),
 col = c("red", "grey"),col.axis = NULL,
 xgrid = FALSE,
 ygrid = FALSE,
 output_data = FALSE,
  ...
\mathcal{L}IncrementalPlot(
  x,
  quantiles = c(0.05, 0.95),
```

```
col = c("red", "grey"),col.axis = NULL,
  xgrid = FALSE,
  ygrid = FALSE,
  output_data = FALSE,
  ...
\mathcal{L}PlotIncremental(
  x,
  quantiles = c(0.05, 0.95),
  col = c("red", "grey"),col.axis = NULL,
  xgrid = FALSE,ygrid = FALSE,
  output_data = FALSE,
  ...
)
```
Arguments

Value

A plot.

See Also

[Incremental](#page-56-0)

plot.roc_band *Receiver Operating Characteristic (ROC) band*

Description

Plots the True Positive Rate (TPR) as a function of the False Positive Rate (FPR) for different thresholds in predicted probabilities. If the results from multiple ROC analyses are provided (e.g. output of [ExplanatoryPerformance](#page-33-0) with large K), the point-wise median is represented and flanked by a transparent band defined by point-wise quantiles. See examples in [ROC](#page-0-0) and [ExplanatoryPerformance](#page-33-0).

plot.variable_selection 81

Usage

```
## S3 method for class 'roc_band'
plot(
  x,
  col_band = NULL,
  alpha = 0.5,
  quantiles = c(0.05, 0.95),
  add = FALSE,...
\mathcal{L}
```
Arguments

Value

A base plot.

See Also

[ROC](#page-0-0), [ExplanatoryPerformance](#page-33-0)

plot.variable_selection

Plot of selection proportions

Description

Makes a barplot of selection proportions in decreasing order. See examples in [VariableSelection](#page-117-0).

Usage

```
## S3 method for class 'variable_selection'
plot(
  x,
 col = c("red", "grey"),col.axis = NULL,
 col.thr = "darkred",
 lty.thr = 2,
 n_predictors = NULL,
  ...
\mathcal{L}
```
Arguments

Value

A plot.

See Also

[VariableSelection](#page-117-0)

PLS *Partial Least Squares 'a la carte'*

Description

Runs a Partial Least Squares (PLS) model in regression mode using algorithm implemented in [pls](#page-0-0). This function allows for the construction of components based on different sets of predictor and/or outcome variables. This function is not using stability.

Usage

```
PLS(
  xdata,
 ydata,
  selectedX = NULL,
  selectedY = NULL,
  family = "gaussian",
  ncomp = NULL,scale = TRUE
```
 \mathcal{L}

Details

All matrices are defined as in (Wold et al. 2001). The weight matrix Wmat is the equivalent of loadings\$X in [pls](#page-0-0). The loadings matrix Pmat is the equivalent of mat.c in [pls](#page-0-0). The score matrices Tmat and Qmat are the equivalent of variates\$X and variates\$Y in [pls](#page-0-0).

Value

A list with:

References

Wold S, Sjöström M, Eriksson L (2001). "PLS-regression: a basic tool of chemometrics." *Chemometrics and Intelligent Laboratory Systems*, 58(2), 109-130. ISSN 0169-7439, [doi:10.1016/S0169-](https://doi.org/10.1016/S0169-7439%2801%2900155-1) [7439\(01\)001551,](https://doi.org/10.1016/S0169-7439%2801%2900155-1) PLS Methods.

See Also

[VariableSelection](#page-117-0), [BiSelection](#page-7-0)

```
if (requireNamespace("mixOmics", quietly = TRUE)) {
 oldpar <- par(no.readonly = TRUE)
 # Data simulation
 set.seed(1)
 simul \le SimulateRegression(n = 200, pk = 15, q = 3, family = "gaussian")
 x <- simul$xdata
 y <- simul$ydata
 # PLS
 mypls \leq PLS(xdata = x, ydata = y, ncomp = 3)
 if (requireNamespace("sgPLS", quietly = TRUE)) {
   # Sparse PLS to identify relevant variables
   stab <- BiSelection(
     xdata = x, ydata = y,
     family = "gaussian", ncomp = 3,
     LambdaX = seq\_len(ncol(x) - 1),
     LambdaY = seq\_len(ncol(y) - 1),
     implementation = SparsePLS,
     n_{cat} = 2\lambdaplot(stab)
   # Refitting of PLS model
   mypls <- PLS(
      xdata = x, ydata = y,
      selectedX = stab$selectedX,
      selectedY = stab$selectedY
   )
   # Nonzero entries in weights are the same as in selectedX
   par(mfrow = c(2, 2))Heatmap(stab$selectedX,
     legend = FALSE
   \lambdatitle("Selected in X")
   Heatmap(ifelse(mypls$Wmat != 0, yes = 1, no = 0),
     legend = FALSE
    )
    title("Nonzero entries in Wmat")
   Heatmap(stab$selectedY,
     legend = FALSE
   \lambdatitle("Selected in Y")
   Heatmap(ifelse(mypls$Cmat != 0, yes = 1, no = 0),
     legend = FALSE
```
predict.variable_selection 85

```
\lambdatitle("Nonzero entries in Cmat")
 }
 # Multilevel PLS
 # Generating random design
 z \leftarrow rep(seq\_len(50), each = 4)# Extracting the within-variability
 x_within <- mixOmics::withinVariation(X = x, design = cbind(z))
 # Running PLS on within-variability
 mypls \leq PLS(xdata = x_within, ydata = y, ncomp = 3)
 par(oldpar)
}
```
predict.variable_selection

Predict method for stability selection

Description

Computes predicted values from the output of [VariableSelection](#page-117-0).

Usage

```
## S3 method for class 'variable_selection'
predict(
  object,
  xdata,
  ydata,
  newdata = NULL,
  method = c("ensemble", "refit"),
  ...
\mathcal{L}
```


Value

Predicted values.

See Also

[Refit](#page-87-0), [Ensemble](#page-31-0), [EnsemblePredictions](#page-32-0)

```
## Linear regression
# Data simulation
set.seed(1)
simul \le SimulateRegression(n = 500, pk = 50, family = "gaussian")
# Training/test split
ids \le Split(data = simul$ydata, tau = c(0.8, 0.2))
# Stability selection
stab <- VariableSelection(
 xdata = simu1$xdata[ids[[1]], ],
 ydata = simul$ydata[ids[[1]], ]
\lambda# Predictions from post stability selection estimation
yhat <- predict(stab,
 xdata = simul$xdata[ids[[1]], ],
 ydata = simul$ydata[ids[[1]], ],
 newdata = simul$xdata[ids[[2]], ],
 method = "refit"
\mathcal{L}cor(simul$ydata[ids[[2]], ], yhat)^2 # Q-squared
# Predictions from ensemble model
yhat <- predict(stab,
  xdata = simul$xdata[ids[[1]], ],
  ydata = simul$ydata[ids[[1]], ],
 newdata = simul$xdata[ids[[2]], ],
  method = "ensemble"
)
cor(simul$ydata[ids[[2]], ], yhat)^2 # Q-squared
## Logistic regression
# Data simulation
set.seed(1)
simul \le SimulateRegression(n = 500, pk = 20, family = "binomial", ev_xy = 0.9)
# Training/test split
ids \le Split(data = simul$ydata, family = "binomial", tau = c(0.8, 0.2))
```
PredictPLS 87

```
# Stability selection
stab <- VariableSelection(
  xdata = simul$xdata[ids[[1]], ],
  ydata = simul$ydata[ids[[1]], ],
  family = "binomial"
\lambda# Predictions from post stability selection estimation
yhat <- predict(stab,
  xdata = simul$xdata[ids[[1]], ],
  ydata = simul$ydata[ids[[1]], ],
  newdata = simul$xdata[ids[[2]], ],
  method = "refit", type = "response"
\lambdaplot(ROC(predicted = yhat, observed = simul$ydata[ids[[2]], ]))
# Predictions from ensemble model
yhat <- predict(stab,
  xdata = simul$xdata[ids[[1]], ],
  ydata = simul$ydata[ids[[1]], ],
 newdata = simul$xdata[ids[[2]], ],
  method = "ensemble", type = "response"
\mathcal{L}plot(ROC(predicted = yhat, observed = simul$ydata[ids[[2]], ]),
  add = TRUE,col = "blue"
)
```
PredictPLS *Partial Least Squares predictions*

Description

Computes predicted values from a Partial Least Squares (PLS) model in regression mode applied on xdata. This function is using the algorithm implemented in [predict.pls](#page-0-0).

Usage

```
PredictPLS(xdata, model)
```
Arguments

Value

An array of predicted values.

See Also

[PLS](#page-81-0)

Examples

```
if (requireNamespace("mixOmics", quietly = TRUE)) {
 # Data simulation
 set.seed(1)
 simul \le SimulateRegression(n = 100, pk = c(5, 5, 5), family = "gaussian")
 x <- simul$xdata
 y <- simul$ydata
 # PLS
 mypls \leq PLS(xdata = x, ydata = y, ncomp = 3)
 # Predicted values
 predicted <- PredictPLS(xdata = x, model = mypls)
}
```
Refit *Regression model refitting*

Description

Refits the regression model with stably selected variables as predictors (without penalisation). Variables in xdata not evaluated in the stability selection model will automatically be included as predictors.

Usage

```
Refit(
  xdata,
  ydata,
  stability = NULL,
  family = NULL,
  implementation = NULL,
 Lambda = NULL,
  seed = 1,
  verbose = TRUE,
  ...
)
Recalibrate(
  xdata,
 ydata,
  stability = NULL,
  family = NULL,
  implementation = NULL,
```
$Refit$ 89

```
Lambda = NULL,seed = 1,
  verbose = TRUE,
  ...
\mathcal{L}
```
Arguments

Value

The output as obtained from:

```
\link[stats]{lm}
                 for linear regression ("gaussian" family).
\link[survival]{coxph}
                 for Cox regression ("cox" family).
\link[stats]{glm}
                 for logistic regression ("binomial" family).
\link[nnet]{multinom}
                 for multinomial regression ("multinomial" family).
```
See Also

[VariableSelection](#page-117-0)

```
## Linear regression
# Data simulation
set.seed(1)
simul \le SimulateRegression(n = 100, pk = 50, family = "gaussian")
# Data split
ids_train <- Resample(
  data = simul$ydata,
  tau = 0.5, family = "gaussian"
)
xtrain <- simul$xdata[ids_train, , drop = FALSE]
ytrain <- simul$ydata[ids_train, , drop = FALSE]
xrefit <- simul$xdata[-ids_train, , drop = FALSE]
yrefit <- simul$ydata[-ids_train, , drop = FALSE]
# Stability selection
stab <- VariableSelection(xdata = xtrain, ydata = ytrain, family = "gaussian")
print(SelectedVariables(stab))
# Refitting the model
refitted <- Refit(
 xdata = xrefit, ydata = yrefit,
  stability = stab
\lambdarefitted$coefficients # refitted coefficients
head(refitted$fitted.values) # refitted predicted values
# Fitting the full model (including all possible predictors)
refitted <- Refit(
  xdata = simul$xdata, ydata = simul$ydata,
  family = "gaussian"
)
refitted$coefficients # refitted coefficients
## Logistic regression
# Data simulation
set.seed(1)
simul \le SimulateRegression(n = 200, pk = 20, family = "binomial")
# Data split
ids_train <- Resample(
  data = simul$ydata,
  tau = 0.5, family = "binomial"
)
xtrain <- simul$xdata[ids_train, , drop = FALSE]
ytrain <- simul$ydata[ids_train, , drop = FALSE]
xrefit <- simul$xdata[-ids_train, , drop = FALSE]
yrefit <- simul$ydata[-ids_train, , drop = FALSE]
```
Resample 91

```
# Stability selection
stab <- VariableSelection(xdata = xtrain, ydata = ytrain, family = "binomial")
# Refitting the model
refitted <- Refit(
 xdata = xrefit, ydata = yrefit,
 stability = stab
\lambdarefitted$coefficients # refitted coefficients
head(refitted$fitted.values) # refitted predicted probabilities
## Partial Least Squares (multiple components)
if (requireNamespace("sgPLS", quietly = TRUE)) {
 # Data simulation
 set.seed(1)
 simul \le SimulateRegression(n = 500, pk = 15, q = 3, family = "gaussian")
 # Data split
 ids_train <- Resample(
   data = simul$ydata,
   tau = 0.5, family = "gaussian"
 \lambdaxtrain <- simul$xdata[ids_train, , drop = FALSE]
 ytrain <- simul$ydata[ids_train, , drop = FALSE]
 xrefit <- simul$xdata[-ids_train, , drop = FALSE]
 yrefit <- simul$ydata[-ids_train, , drop = FALSE]
 # Stability selection
 stab <- BiSelection(
   xdata = xtrain, ydata = ytrain,
   family = "gaussian", ncomp = 3,
   LambdaX = seq\_len(ncol(xtrain) - 1),
   LambdaY = seq\_len(ncol(ytrain) - 1),
   implementation = SparsePLS
 \lambdaplot(stab)
 # Refitting the model
 refitted <- Refit(
   xdata = xrefit, ydata = yrefit,
   stability = stab
 )
 refitted$Wmat # refitted X-weights
 refitted$Cmat # refitted Y-weights
}
```
Description

Generates a vector of resampled observation IDs.

Usage

```
Resample(data, family = NULL, tau = 0.5, resampling = "subsampling", ...)
```
Arguments

Details

With categorical outcomes (i.e. "family" argument is set to "binomial", "multinomial" or "cox"), the resampling is done such that the proportion of observations from each of the categories is representative of that of the full sample.

Value

A vector of resampled IDs.

```
## Linear regression framework
# Data simulation
simul <- SimulateRegression()
# Subsampling
ids <- Resample(data = simul$ydata, family = "gaussian")
sum(duplicated(ids))
# Bootstrapping
ids <- Resample(data = simul$ydata, family = "gaussian", resampling = "bootstrap")
sum(duplicated(ids))
## Logistic regression framework
# Data simulation
simul <- SimulateRegression(family = "binomial")
```
SelectionAlgo 93

```
# Subsampling
ids <- Resample(data = simul$ydata, family = "binomial")
sum(duplicated(ids))
prop.table(table(simul$ydata))
prop.table(table(simul$ydata[ids]))
# Data simulation for a binary confounder
conf <- ifelse(runif(n = 100) > 0.5, yes = 1, no = 0)
# User-defined resampling function
BalancedResampling <- function(data, tau, Z, ...) {
  s <- NULL
  for (z \in \text{in unique}(Z)) {
  s <- c(s, sample(which((data == "0") & (Z == z)), size = tau * sum((data == "0") & (Z == z))))
  s <- c(s, sample(which((data == "1") & (Z == z)), size = tau * sum((data == "1") & (Z == z))))
  }
  return(s)
}
# Resampling keeping proportions by Y and Z
ids <- Resample(data = simul$ydata, family = "binomial", resampling = BalancedResampling, Z = conf)
prop.table(table(simul$ydata, conf))
prop.table(table(simul$ydata[ids], conf[ids]))
# User-defined resampling for stability selection
stab <- VariableSelection(
  xdata = simul$xdata, ydata = simul$ydata, family = "binomial",
  resampling = BalancedResampling, Z = conf
\mathcal{L}
```
SelectionAlgo *Variable selection algorithm*

Description

Runs the variable selection algorithm specified in the argument implementation. This function is not using stability.

Usage

```
SelectionAlgo(
  xdata,
  ydata = NULL,
  Lambda,
  group_x = NULL,
  scale = TRUE,
  family = NULL,implementation = PenalisedRegression,
  ...
)
```
Arguments

Value

A list with:

See Also

[VariableSelection](#page-117-0), [PenalisedRegression](#page-74-0), [SparsePCA](#page-100-0), [SparsePLS](#page-102-0), [GroupPLS](#page-52-0), [SparseGroupPLS](#page-98-0) Other wrapping functions: [GraphicalAlgo\(](#page-44-0))

```
# Data simulation (univariate outcome)
set.seed(1)
simul <- SimulateRegression(pk = 50)
# Running the LASSO
mylasso <- SelectionAlgo(
 xdata = simul$xdata, ydata = simul$ydata,
  Lambda = c(0.1, 0.2), family = "gaussian",
\mathcal{L}
```
SelectionPerformance 95

```
# Data simulation (multivariate outcome)
set.seed(1)
simul <- SimulateRegression(pk = 50, q = 3)
# Running multivariate Gaussian LASSO
mylasso <- SelectionAlgo(
  xdata = simul$xdata, ydata = simul$ydata,
  Lambda = c(0.1, 0.2), family = "mgaussian"
)
str(mylasso)
```
SelectionPerformance *Selection performance*

Description

Computes different metrics of selection performance by comparing the set of selected features to the set of true predictors/edges. This function can only be used in simulation studies (i.e. when the true model is known).

Usage

```
SelectionPerformance(theta, theta_star, pk = NULL, cor = NULL, thr = 0.5)
```
Arguments

Value

A matrix of selection metrics including:

- TP number of True Positives (TP)
- FN number of False Negatives (TN)
- FP number of False Positives (FP)

If argument "cor" is provided, the number of False Positives among correlated (FP_c) and uncorrelated (FP_i) pairs, defined as having correlations (provided in "cor") above or below the threshold "thr", are also reported.

Block-specific performances are reported if "pk" is not NULL. In this case, the first row of the matrix corresponds to the overall performances, and subsequent rows correspond to each of the blocks. The order of the blocks is defined as in [BlockStructure](#page-0-0).

See Also

Other functions for model performance: [ClusteringPerformance\(](#page-24-0)), [SelectionPerformanceGraph\(](#page-95-0))

Examples

```
# Variable selection model
set.seed(1)
simul <- SimulateRegression(pk = 30, nu_xy = 0.5)
stab <- VariableSelection(xdata = simul$xdata, ydata = simul$ydata)
# Selection performance
SelectionPerformance(theta = stab, theta_star = simul)
# Alternative formulation
SelectionPerformance(
  theta = SelectedVariables(stab),
  theta_star = simul$theta
)
```
SelectionPerformanceGraph

Graph representation of selection performance

Description

Generates an igraph object representing the True Positive, False Positive and False Negative edges by comparing the set of selected edges to the set of true edges. This function can only be used in simulation studies (i.e. when the true model is known).

SelectionPerformanceGraph 97

Usage

```
SelectionPerformanceGraph(
  theta,
  theta_star,
 col = c("tomato", "forestgreen", "navy"),
 lty = c(2, 3, 1),node_colour = NULL,
  show_labels = TRUE,
  ...
\mathcal{L}
```
Arguments

Value

An igraph object.

See Also

[SimulateGraphical](#page-0-0), [SimulateRegression](#page-0-0), [GraphicalModel](#page-45-0), [VariableSelection](#page-117-0), [BiSelection](#page-7-0) Other functions for model performance: [ClusteringPerformance\(](#page-24-0)), [SelectionPerformance\(](#page-94-0))

```
# Data simulation
set.seed(1)
simul <- SimulateGraphical(pk = 30)
# Stability selection
stab <- GraphicalModel(xdata = simul$data, K = 10)
# Performance graph
perfgraph <- SelectionPerformanceGraph(
```

```
theta = stab,
  theta_star = simul
)
plot(perfgraph)
```
SelectionProportions *Selection/co-membership proportions*

Description

Extracts selection proportions (for stability selection) or co-membership proportions (for consensus clustering).

Usage

```
SelectionProportions(stability, argmax_id = NULL)
```
ConsensusMatrix(stability, argmax_id = NULL)

Arguments

Value

A vector or matrix of proportions.

See Also

[VariableSelection](#page-117-0), [GraphicalModel](#page-45-0), [BiSelection](#page-7-0), [Clustering](#page-19-0)

```
# Stability selection
set.seed(1)
simul <- SimulateRegression(pk = 50)
stab <- VariableSelection(xdata = simul$xdata, ydata = simul$ydata)
SelectionProportions(stab)
# Consensus clustering
set.seed(1)
simul <- SimulateClustering(
 n = c(30, 30, 30), nu\_xc = 1, ev\_xc = 0.5\lambdastab <- Clustering(xdata = simul$data)
```
SparseGroupPLS 99

ConsensusMatrix(stab)

SparseGroupPLS *Sparse group Partial Least Squares*

Description

Runs a sparse group Partial Least Squares model using implementation from [sgPLS-package](#page-0-0). This function is not using stability.

Usage

```
SparseGroupPLS(
  xdata,
 ydata,
  family = "gaussian",
 group_x,
 group_y = NULL,Lambda,
  alpha.x,
  alpha.y = NULL,
 keepX_previous = NULL,
 keepY = NULL,
 ncomp = 1,
  scale = TRUE,
  ...
)
```


Value

A list with:

References

Liquet B, de Micheaux PL, Hejblum BP, Thiébaut R (2016). "Group and sparse group partial least square approaches applied in genomics context." *Bioinformatics*, 32(1), 35-42. ISSN 1367-4803, [doi:10.1093/bioinformatics/btv535.](https://doi.org/10.1093/bioinformatics/btv535)

See Also

[VariableSelection](#page-117-0), [BiSelection](#page-7-0)

Other penalised dimensionality reduction functions: [GroupPLS\(](#page-52-0)), [SparsePCA\(](#page-100-0)), [SparsePLS\(](#page-102-0))

```
if (requireNamespace("sgPLS", quietly = TRUE)) {
  ## Sparse group PLS
  # Data simulation
  set.seed(1)
  simul \le SimulateRegression(n = 100, pk = 30, q = 3, family = "gaussian")
  x <- simul$xdata
  y <- simul$ydata
  # Running sgPLS with 1 group and sparsity of 0.5
  mypls <- SparseGroupPLS(
   xdata = x, ydata = y, Lambda = 1, family = "gaussian",group_x = c(10, 15, 5), alpha.x = 0.5
  \lambda
```
SparsePCA 101

```
# Running sgPLS with groups on outcomes
 mypls <- SparseGroupPLS(
   xdata = x, ydata = y, Lambda = 1, family = "gaussian",group_x = c(10, 15, 5), alpha.x = 0.5,group_y = c(2, 1), keepY = 1, alpha.y = 0.9\overline{)}## Sparse group PLS-DA
 # Data simulation
 set.seed(1)
 simul <- SimulateRegression(n = 100, pk = 50, family = "binomial")
 # Running sgPLS-DA with 1 group and sparsity of 0.9
 mypls <- SparseGroupPLS(
   xdata = simul$xdata, ydata = simul$ydata, Lambda = 1, family = "binomial",
   group_x = c(10, 15, 25), alpha.x = 0.9)
}
```


SparsePCA *Sparse Principal Component Analysis*

Description

Runs a sparse Principal Component Analysis model using implementation from [spca](#page-0-0) (if algo="sPCA") or [spca](#page-0-0) (if algo="rSVD"). This function is not using stability.

Usage

```
SparsePCA(
 xdata,
 Lambda,
 ncomp = 1,
  scale = TRUE,
 keepX_previous = NULL,
 algorithm = "sPCA",
  ...
)
```


Value

References

Zou H, Hastie T, Tibshirani R (2006). "Sparse Principal Component Analysis." *Journal of Computational and Graphical Statistics*, 15(2), 265-286. [doi:10.1198/106186006X113430.](https://doi.org/10.1198/106186006X113430)

Shen H, Huang JZ (2008). "Sparse principal component analysis via regularized low rank matrix approximation." *Journal of Multivariate Analysis*, 99(6), 1015-1034. ISSN 0047-259X, [doi:10.1016/](https://doi.org/10.1016/j.jmva.2007.06.007) [j.jmva.2007.06.007.](https://doi.org/10.1016/j.jmva.2007.06.007)

See Also

[VariableSelection](#page-117-0), [BiSelection](#page-7-0)

Other penalised dimensionality reduction functions: [GroupPLS\(](#page-52-0)), [SparseGroupPLS\(](#page-98-0)), [SparsePLS\(](#page-102-0))

```
# Data simulation
set.seed(1)
simul <- SimulateRegression(n = 100, pk = 50, family = "gaussian")
x <- simul$xdata
# Sparse PCA (by Zou, Hastie, Tibshirani)
if (requireNamespace("elasticnet", quietly = TRUE)) {
  mypca <- SparsePCA(
   xdata = x, ncomp = 2,
   Lambda = c(1, 2), keepX_previous = 10, algorithm = "sPCA"
  )
}
# Sparse PCA (by Shen and Huang)
if (requireNamespace("mixOmics", quietly = TRUE)) {
 mypca <- SparsePCA(
   xdata = x, ncomp = 2,
```

```
Lambda = c(1, 2), keepX_previous = 10, algorithm = "rSVD"
 )
}
```


SparsePLS *Sparse Partial Least Squares*

Description

Runs a sparse Partial Least Squares model using implementation from [sgPLS-package](#page-0-0). This function is not using stability.

Usage

```
SparsePLS(
 xdata,
 ydata,
 Lambda,
  family = "gaussian",
 ncomp = 1,
  scale = TRUE,keepX_previous = NULL,
 keepY = NULL,
  ...
)
```


Value

References

KA LC, Rossouw D, Robert-Granié C, Besse P (2008). "A sparse PLS for variable selection when integrating omics data." *Stat Appl Genet Mol Biol*, 7(1), Article 35. ISSN 1544-6115, [doi:10.2202/](https://doi.org/10.2202/1544-6115.1390) [15446115.1390.](https://doi.org/10.2202/1544-6115.1390)

See Also

[VariableSelection](#page-117-0), [BiSelection](#page-7-0)

Other penalised dimensionality reduction functions: [GroupPLS\(](#page-52-0)), [SparseGroupPLS\(](#page-98-0)), [SparsePCA\(](#page-100-0))

```
if (requireNamespace("sgPLS", quietly = TRUE)) {
 ## Sparse PLS
 # Data simulation
 set.seed(1)
 simul \le SimulateRegression(n = 100, pk = 20, q = 3, family = "gaussian")
 x <- simul$xdata
 y <- simul$ydata
 # Running sPLS with 2 X-variables and 1 Y-variable
 mypls <- SparsePLS(xdata = x, ydata = y, Lambda = 2, family = "gaussian", keepY = 1)
 ## Sparse PLS-DA
 # Data simulation
 set.seed(1)
 simul <- SimulateRegression(n = 100, pk = 20, family = "binomial")
 # Running sPLS-DA with 2 X-variables and 1 Y-variable
 mypls <- SparsePLS(xdata = simul$xdata, ydata = simul$ydata, Lambda = 2, family = "binomial")
}
```
Description

Generates a list of length(tau) non-overlapping sets of observation IDs.

Usage

 $Split(data, family = NULL, tau = c(0.5, 0.25, 0.25)$

Arguments

Details

With categorical outcomes (i.e. family argument is set to "binomial", "multinomial" or "cox"), the split is done such that the proportion of observations from each of the categories in each of the sets is representative of that of the full sample.

Value

A list of length length(tau) with sets of non-overlapping observation IDs.

```
# Splitting into 3 sets
simul <- SimulateRegression()
ids <- Split(data = simul$ydata)
lapply(ids, length)
# Balanced splits with respect to a binary variable
simul <- SimulateRegression(family = "binomial")
ids <- Split(data = simul$ydata, family = "binomial")
lapply(ids, FUN = function(x) {
  table(simul$ydata[x, ])
})
```
Description

Generates a symmetric adjacency matrix encoding a bipartite graph.

Usage

Square(x)

Arguments

x matrix encoding the edges between two types of nodes (rows and columns).

Value

A symmetric adjacency matrix encoding a bipartite graph.

Examples

```
# Simulated links between two sets
set.seed(1)
mat \le matrix(sample(c(0, 1), size = 15, replace = TRUE),
  nrow = 5, ncol = 3)
# Adjacency matrix of a bipartite graph
Square(mat)
```
StabilityMetrics *Stability selection metrics*

Description

Computes the stability score (see [StabilityScore](#page-109-0)) and upper-bounds of the [PFER](#page-76-0) and [FDP](#page-37-0) from selection proportions of models with a given parameter controlling the sparsity of the underlying algorithm and for different thresholds in selection proportions.

StabilityMetrics 107

Usage

```
StabilityMetrics(
  selprop,
  pk = NULL,
  pi_list = seq(0.6, 0.9, by = 0.01),K = 100,n_{cat} = NULL,
  PFER_method = "MB",
  PFER_thr_blocks = Inf,
  FDP_thr_blocks = Inf,
  Sequential_template = NULL,
  graph = TRUE,group = NULL\mathcal{L}
```


Value

FDP_2d an array of computed upper-bounds of FDP obtained with different combinations of parameters. Rows correspond to different penalty parameters and columns correspond to different thresholds in selection proportions. Not available in multi-block stability selection graphical modelling.

References

Bodinier B, Filippi S, Nøst TH, Chiquet J, Chadeau-Hyam M (2023). "Automated calibration for stability selection in penalised regression and graphical models." *Journal of the Royal Statistical Society Series C: Applied Statistics*, qlad058. ISSN 0035-9254, [doi:10.1093/jrsssc/qlad058,](https://doi.org/10.1093/jrsssc/qlad058) https://academic.oup.com/jrsssc/advance-article-pdf/doi/10.1093/jrsssc/qlad058/50878777/qlad058.pdf.

Meinshausen N, Bühlmann P (2010). "Stability selection." *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 72(4), 417-473. [doi:10.1111/j.14679868.2010.00740.x.](https://doi.org/10.1111/j.1467-9868.2010.00740.x)

Shah RD, Samworth RJ (2013). "Variable selection with error control: another look at stability selection." *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 75(1), 55- 80. [doi:10.1111/j.14679868.2011.01034.x.](https://doi.org/10.1111/j.1467-9868.2011.01034.x)

See Also

Other stability metric functions: [ConsensusScore\(](#page-28-0)), [FDP\(](#page-37-0)), [PFER\(](#page-76-0)), [StabilityScore\(](#page-109-0))

```
## Sparse or sparse group penalisation
```

```
# Simulating set of selection proportions
set.seed(1)
selprop \leq matrix(round(runif(n = 20), digits = 2), nrow = 2)
# Computing stability scores for different thresholds
metrics <- StabilityMetrics(
  selfprop = selfprop, pi = c(0.6, 0.7, 0.8),K = 100, graph = FALSE
)
## Group penalisation
# Simulating set of selection proportions
set.seed(1)
selprop \leq matrix(round(runif(n = 6), digits = 2), nrow = 2)
selprop <- cbind(
  selprop[, 1], selprop[, 1],
  selprop[, 2], selprop[, 2],
  matrix(rep(selfprop[, 3], each = 6), nrow = 2, byrow = TRUE))
# Computing stability scores for different thresholds
metrics <- StabilityMetrics(
  selfprop = selfprop, pi = c(0.6, 0.7, 0.8),K = 100, graph = FALSE, group = c(2, 2, 6)
```
StabilityScore *Stability score*

Description

Computes the stability score from selection proportions of models with a given parameter controlling the sparsity and for different thresholds in selection proportions. The score measures how unlikely it is that the selection procedure is uniform (i.e. uninformative) for a given combination of parameters.

Usage

```
StabilityScore(
  selprop,
  pi_list = seq(0.6, 0.9, by = 0.01),
 K,
  n_{cat} = 3,
  group = NULL
)
```
Arguments

Details

The stability score is derived from the likelihood under the assumption of uniform (uninformative) selection.

We classify the features into three categories: the stably selected ones (that have selection proportions $\geq \pi$), the stably excluded ones (selection proportion $\leq 1-\pi$), and the unstable ones (selection proportions between $1 - \pi$ and π).

Under the hypothesis of equiprobability of selection (instability), the likelihood of observing stably selected, stably excluded and unstable features can be expressed as:

 \mathcal{L}

Stable 111

$$
L_{\lambda,\pi} = \prod_{j=1}^{N} [(1 - F(K\pi - 1))^{1_{H_{\lambda}(j) \ge K\pi}} \times (F(K\pi - 1) - F(K(1 - \pi))^{1_{(1-\pi)K < H_{\lambda}(j) < K\pi}} \times F(K(1 - \pi))^{1_{H_{\lambda}(j) \le K(1-\pi)}}]
$$

where $H_{\lambda}(j)$ is the selection count of feature j and $F(x)$ is the cumulative probability function of the binomial distribution with parameters K and the average proportion of selected features over resampling iterations.

The stability score is computed as the minus log-transformed likelihood under the assumption of equiprobability of selection:

 $S_{\lambda,\pi} = -log(L_{\lambda,\pi})$

The stability score increases with stability.

Alternatively, the stability score can be computed by considering only two sets of features: stably selected (selection proportions $\geq \pi$) or not (selection proportions $\lt \pi$). This can be done using n_cat=2.

Value

A vector of stability scores obtained with the different thresholds in selection proportions.

References

Bodinier B, Filippi S, Nøst TH, Chiquet J, Chadeau-Hyam M (2023). "Automated calibration for stability selection in penalised regression and graphical models." *Journal of the Royal Statistical Society Series C: Applied Statistics*, qlad058. ISSN 0035-9254, [doi:10.1093/jrsssc/qlad058,](https://doi.org/10.1093/jrsssc/qlad058) https://academic.oup.com/jrsssc/advance-article-pdf/doi/10.1093/jrsssc/qlad058/50878777/qlad058.pdf.

See Also

Other stability metric functions: [ConsensusScore\(](#page-28-0)), [FDP\(](#page-37-0)), [PFER\(](#page-76-0)), [StabilityMetrics\(](#page-105-0))

Examples

```
# Simulating set of selection proportions
set.seed(1)
selprop \le round(runif(n = 20), digits = 2)
# Computing stability scores for different thresholds
score <- StabilityScore(selprop, pilist = c(0.6, 0.7, 0.8), K = 100)
```
Stable *Stable results*

Description

Extracts stable results for stability selection or consensus clustering.

Usage

```
Stable(stability, argmax_id = NULL, linkage = "complete")
SelectedVariables(stability, argmax_id = NULL)
Adjacency(stability, argmax_id = NULL)
Clusters(stability, linkage = "complete", argmax_id = NULL)
```
Arguments

Value

A binary vector or matrix encoding the selection status (1 if selected, 0 otherwise) in stability selection or stable cluster membership in consensus clustering.

See Also

[VariableSelection](#page-117-0), [BiSelection](#page-7-0), [GraphicalModel](#page-45-0), [Clustering](#page-19-0)

```
# Variable selection
set.seed(1)
simul <- SimulateRegression(pk = 20)
stab <- VariableSelection(xdata = simul$xdata, ydata = simul$ydata)
SelectedVariables(stab)
Stable(stab)
# Graphical model
set.seed(1)
simul <- SimulateGraphical(pk = 10)
stab <- GraphicalModel(xdata = simul$data)
Adjacency(stab)
Stable(stab)
# Clustering
set.seed(1)
simul <- SimulateClustering(
 n = c(30, 30, 30),
 nu_xc = 1\lambdastab <- Clustering(xdata = simul$data)
```
Clusters(stab) Stable(stab)

StructuralModel *Stability selection in Structural Equation Modelling*

Description

Performs stability selection for Structural Equation Models. The underlying arrow selection algorithm (e.g. regularised Structural Equation Modelling) is run with different combinations of parameters controlling the sparsity (e.g. penalty parameter) and thresholds in selection proportions. These two hyper-parameters are jointly calibrated by maximisation of the stability score.

Usage

```
StructuralModel(
  xdata,
  adjacency,
  residual_covariance = NULL,
  Lambda = NULL,pi_list = seq(0.01, 0.99, by = 0.01),
 K = 100.
  tau = 0.5,
  seed = 1,
  n_{cat} = NULL,
  implementation = PenalisedLinearSystem,
  resampling = "subsampling",
  cpss = FALSE,PFER_method = "MB",
 PFER_thr = Inf,
  FDP_{thr} = Inf,Lambda_cardinal = 100,
 optimisation = c("grid_search", "nloptr"),
  n\_cores = 1,output_data = FALSE,
  verbose = TRUE,
  ...
\lambda
```
Arguments

- Lambda matrix of parameters controlling the level of sparsity in the underlying feature selection algorithm specified in implementation.
- pi_list vector of thresholds in selection proportions. If n_cat=NULL or n_cat=2, these values must be >0 and <1. If n_cat=3, these values must be >0.5 and <1.
- K number of resampling iterations.
- tau subsample size. Only used if resampling="subsampling" and cpss=FALSE.
- seed value of the seed to initialise the random number generator and ensure reproducibility of the results (see set. seed).
- n_cat computation options for the stability score. Default is NULL to use the score based on a z test. Other possible values are 2 or 3 to use the score based on the negative log-likelihood.

implementation function to use for variable selection.

- resampling resampling approach. Possible values are: "subsampling" for sampling without replacement of a proportion tau of the observations, or "bootstrap" for sampling with replacement generating a resampled dataset with as many observations as in the full sample. Alternatively, this argument can be a function to use for resampling. This function must use arguments named data and tau and return the IDs of observations to be included in the resampled dataset.
- cpss logical indicating if complementary pair stability selection should be done. For this, the algorithm is applied on two non-overlapping subsets of half of the observations. A feature is considered as selected if it is selected for both subsamples. With this method, the data is split K/2 times (K models are fitted). Only used if PFER_method="MB".
- PFER_method method used to compute the upper-bound of the expected number of False Positives (or Per Family Error Rate, PFER). If PFER_method="MB", the method proposed by Meinshausen and Bühlmann (2010) is used. If PFER_method="SS", the method proposed by Shah and Samworth (2013) under the assumption of unimodality is used.
- PFER_thr threshold in PFER for constrained calibration by error control. If PFER_thr=Inf and FDP_thr=Inf, unconstrained calibration is used (the default).
- FDP_{_thr} threshold in the expected proportion of falsely selected features (or False Discovery Proportion) for constrained calibration by error control. If PFER_thr=Inf and FDP_thr=Inf, unconstrained calibration is used (the default).

Lambda_cardinal

optimisation character string indicating the type of optimisation method. With optimisation="grid_search" (the default), all values in Lambda are visited. Alternatively, optimisation algorithms implemented in [nloptr](#page-0-0) can be used with optimisation="nloptr". By default, we use "algorithm"="NLOPT_GN_DIRECT_L", "xtol_abs"=0.1, "ftol_abs"=0.1 and "maxeval"=Lambda_cardinal. These values can be changed

Details

In stability selection, a feature selection algorithm is fitted on K subsamples (or bootstrap samples) of the data with different parameters controlling the sparsity (Lambda). For a given (set of) sparsity parameter(s), the proportion out of the K models in which each feature is selected is calculated. Features with selection proportions above a threshold pi are considered stably selected. The stability selection model is controlled by the sparsity parameter(s) for the underlying algorithm, and the threshold in selection proportion:

 $V_{\lambda,\pi} = \{j : p_{\lambda}(j) \geq \pi\}$

In Structural Equation Modelling, "feature" refers to an arrow in the corresponding Directed Acyclic Graph.

These parameters can be calibrated by maximisation of a stability score (see [ConsensusScore](#page-28-0) if n_cat=NULL or [StabilityScore](#page-109-0) otherwise) calculated under the null hypothesis of equiprobability of selection.

It is strongly recommended to examine the calibration plot carefully to check that the grids of parameters Lambda and pi_list do not restrict the calibration to a region that would not include the global maximum (see [CalibrationPlot](#page-15-0)). In particular, the grid Lambda may need to be extended when the maximum stability is observed on the left or right edges of the calibration heatmap. In some instances, multiple peaks of stability score can be observed. Simulation studies suggest that the peak corresponding to the largest number of selected features tend to give better selection performances. This is not necessarily the highest peak (which is automatically retained by the functions in this package). The user can decide to manually choose another peak.

To control the expected number of False Positives (Per Family Error Rate) in the results, a threshold PFER_thr can be specified. The optimisation problem is then constrained to sets of parameters that generate models with an upper-bound in PFER below PFER_thr (see Meinshausen and Bühlmann (2010) and Shah and Samworth (2013)).

Possible resampling procedures include defining (i) K subsamples of a proportion tau of the observations, (ii) K bootstrap samples with the full sample size (obtained with replacement), and (iii) K/2 splits of the data in half for complementary pair stability selection (see arguments resampling and cpss). In complementary pair stability selection, a feature is considered selected at a given resampling iteration if it is selected in the two complementary subsamples.

To ensure reproducibility of the results, the starting number of the random number generator is set to seed.

For parallelisation, stability selection with different sets of parameters can be run on n_cores cores. Using n_cores > 1 creates a [multisession](#page-0-0). Alternatively, the function can be run manually with different seeds and all other parameters equal. The results can then be combined using [Combine](#page-26-0).

Value

An object of class variable_selection. A list with:

For all matrices and arrays returned, the rows are ordered in the same way and correspond to parameter values stored in Lambda.

StructuralModel 117

References

Bodinier B, Filippi S, Nøst TH, Chiquet J, Chadeau-Hyam M (2023). "Automated calibration for stability selection in penalised regression and graphical models." *Journal of the Royal Statistical Society Series C: Applied Statistics*, qlad058. ISSN 0035-9254, [doi:10.1093/jrsssc/qlad058,](https://doi.org/10.1093/jrsssc/qlad058) https://academic.oup.com/jrsssc/advance-article-pdf/doi/10.1093/jrsssc/qlad058/50878777/qlad058.pdf.

Meinshausen N, Bühlmann P (2010). "Stability selection." *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 72(4), 417-473. [doi:10.1111/j.14679868.2010.00740.x.](https://doi.org/10.1111/j.1467-9868.2010.00740.x)

Shah RD, Samworth RJ (2013). "Variable selection with error control: another look at stability selection." *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 75(1), 55- 80. [doi:10.1111/j.14679868.2011.01034.x.](https://doi.org/10.1111/j.1467-9868.2011.01034.x)

Jacobucci R, Grimm KJ, McArdle JJ (2016). "Regularized structural equation modeling." *Structural equation modeling: a multidisciplinary journal*, 23(4), 555–566. [doi:10.1080/10705511.2016.1154793.](https://doi.org/10.1080/10705511.2016.1154793)

See Also

[SelectionAlgo](#page-92-0), [Resample](#page-90-0), [StabilityScore](#page-109-0)

Other stability functions: [BiSelection\(](#page-7-0)), [Clustering\(](#page-19-0)), [GraphicalModel\(](#page-45-0)), [VariableSelection\(](#page-117-0))

```
oldpar <- par(no.readonly = TRUE)
par(max = rep(7, 4))# Data simulation
set.seed(1)
pk \leq -c(3, 2, 3)simul <- SimulateStructural(
 n = 500,
  pk = pk,
  nu_between = 0.5,
  v_between = 1,
  v_sign = 1
\lambda# Stability selection (using glmnet)
dag <- LayeredDAG(layers = pk)
stab <- StructuralModel(
  xdata = simul$data,
  adjacency = dag
\lambdaCalibrationPlot(stab)
LinearSystemMatrix(vect = Stable(stab), adjacency = dag)
# Stability selection (using OpenMx)
if (requireNamespace("OpenMx", quietly = TRUE)) {
  stab <- StructuralModel(
    xdata = simul$data,
    implementation = PenalisedOpenMx,
    Lambda = seq(50, 500, by = 50),
```

```
adjacency = dag
 )
 CalibrationPlot(stab)
 OpenMxMatrix(SelectedVariables(stab), adjacency = dag)
}
## Not run:
# Data simulation with latent variables
set.seed(1)
pk <- c(3, 2, 3)
simul <- SimulateStructural(
 n = 500,pk = pk,
 nu_between = 0.5,
 v_sign = 1,
 v_between = 1,
 n_manifest = 3,
 ev_manifest = 0.95
)
# Stability selection (using OpenMx)
if (requireNamespace("OpenMx", quietly = TRUE)) {
 dag <- LayeredDAG(layers = pk, n_manifest = 3)
 penalised <- dag
 penalised[, seq_len(ncol(simul$data))] <- 0
 stab <- StructuralModel(
   xdata = simul$data,
   implementation = PenalisedOpenMx,
   adjacency = dag,
   penalised = penalised,
   Lambda = seq(10, 100, by = 20),
   K = 10 # to increase for real use
 \lambdaCalibrationPlot(stab)
 ids_latent <- grep("f", colnames(dag))
 OpenMxMatrix(SelectedVariables(stab),
    adjacency = dag
 )[ids_latent, ids_latent]
}
## End(Not run)
par(oldpar)
```
VariableSelection *Stability selection in regression*

Description

Performs stability selection for regression models. The underlying variable selection algorithm (e.g. LASSO regression) is run with different combinations of parameters controlling the sparsity (e.g.

VariableSelection 119

penalty parameter) and thresholds in selection proportions. These two hyper-parameters are jointly calibrated by maximisation of the stability score.

Usage

```
VariableSelection(
  xdata,
  ydata = NULL,
 Lambda = NULL,pi_list = seq(0.01, 0.99, by = 0.01),K = 100,
  tau = 0.5,
  seed = 1,
  n_{cat} = NULL,family = "gaussian",
  implementation = PenalisedRegression,
  resampling = "subsampling",
  cpss = FALSE,
  PFER_method = "MB",
 PFER_thr = Inf,
  FDP_{thr} = Inf,Lambda_cardinal = 100,
  group_x = NULL,group_penalisation = FALSE,
  optimisation = c("grid_search", "nloptr"),
  n\_cores = 1,output_data = FALSE,
  verbose = TRUE,
  beep = NULL,
  ...
\mathcal{L}
```
Arguments

Details

In stability selection, a feature selection algorithm is fitted on K subsamples (or bootstrap samples) of the data with different parameters controlling the sparsity (Lambda). For a given (set of) sparsity parameter(s), the proportion out of the K models in which each feature is selected is calculated. Features with selection proportions above a threshold pi are considered stably selected. The stability selection model is controlled by the sparsity parameter(s) for the underlying algorithm, and the threshold in selection proportion:

 $V_{\lambda,\pi} = \{j : p_{\lambda}(j) \geq \pi\}$

If argument group_penalisation=FALSE, "feature" refers to variable (variable selection model). If argument group_penalisation=TRUE, "feature" refers to group (group selection model). In this case, groups need to be defined *a priori* and specified in argument group_x.

These parameters can be calibrated by maximisation of a stability score (see [ConsensusScore](#page-28-0) if n_cat=NULL or [StabilityScore](#page-109-0) otherwise) calculated under the null hypothesis of equiprobability of selection.

It is strongly recommended to examine the calibration plot carefully to check that the grids of parameters Lambda and pi_list do not restrict the calibration to a region that would not include the global maximum (see [CalibrationPlot](#page-15-0)). In particular, the grid Lambda may need to be extended when the maximum stability is observed on the left or right edges of the calibration heatmap. In some instances, multiple peaks of stability score can be observed. Simulation studies suggest that the peak corresponding to the largest number of selected features tend to give better selection performances. This is not necessarily the highest peak (which is automatically retained by the functions in this package). The user can decide to manually choose another peak.

To control the expected number of False Positives (Per Family Error Rate) in the results, a threshold PFER_thr can be specified. The optimisation problem is then constrained to sets of parameters that generate models with an upper-bound in PFER below PFER_thr (see Meinshausen and Bühlmann (2010) and Shah and Samworth (2013)).

Possible resampling procedures include defining (i) K subsamples of a proportion tau of the observations, (ii) K bootstrap samples with the full sample size (obtained with replacement), and (iii) K/2 splits of the data in half for complementary pair stability selection (see arguments resampling and cpss). In complementary pair stability selection, a feature is considered selected at a given resampling iteration if it is selected in the two complementary subsamples.

For categorical or time to event outcomes (argument family is "binomial", "multinomial" or "cox"), the proportions of observations from each category in all subsamples or bootstrap samples are the same as in the full sample.

To ensure reproducibility of the results, the starting number of the random number generator is set to seed.

For parallelisation, stability selection with different sets of parameters can be run on n_cores cores. Using n_cores > 1 creates a [multisession](#page-0-0). Alternatively, the function can be run manually with different seeds and all other parameters equal. The results can then be combined using [Combine](#page-26-0).

Value

An object of class variable_selection. A list with:

For all matrices and arrays returned, the rows are ordered in the same way and correspond to parameter values stored in Lambda.

VariableSelection 123

References

Bodinier B, Filippi S, Nøst TH, Chiquet J, Chadeau-Hyam M (2023). "Automated calibration for stability selection in penalised regression and graphical models." *Journal of the Royal Statistical Society Series C: Applied Statistics*, qlad058. ISSN 0035-9254, [doi:10.1093/jrsssc/qlad058,](https://doi.org/10.1093/jrsssc/qlad058) https://academic.oup.com/jrsssc/advance-article-pdf/doi/10.1093/jrsssc/qlad058/50878777/qlad058.pdf.

Shah RD, Samworth RJ (2013). "Variable selection with error control: another look at stability selection." *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 75(1), 55- 80. [doi:10.1111/j.14679868.2011.01034.x.](https://doi.org/10.1111/j.1467-9868.2011.01034.x)

Meinshausen N, Bühlmann P (2010). "Stability selection." *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 72(4), 417-473. [doi:10.1111/j.14679868.2010.00740.x.](https://doi.org/10.1111/j.1467-9868.2010.00740.x)

Tibshirani R (1996). "Regression Shrinkage and Selection via the Lasso." *Journal of the Royal Statistical Society. Series B (Methodological)*, 58(1), 267–288. ISSN 00359246, [http://www.](http://www.jstor.org/stable/2346178) [jstor.org/stable/2346178](http://www.jstor.org/stable/2346178).

See Also

[PenalisedRegression](#page-74-0), [SelectionAlgo](#page-92-0), [LambdaGridRegression](#page-63-0), [Resample](#page-90-0), [StabilityScore](#page-109-0) [Refit](#page-87-0), [ExplanatoryPerformance](#page-33-0), [Incremental](#page-56-0),

Other stability functions: [BiSelection\(](#page-7-0)), [Clustering\(](#page-19-0)), [GraphicalModel\(](#page-45-0)), [StructuralModel\(](#page-112-0))

```
oldpar <- par(no.readonly = TRUE)
par(max = rep(7, 4))# Linear regression
set.seed(1)
simul \le SimulateRegression(n = 100, pk = 50, family = "gaussian")
stab <- VariableSelection(
  xdata = simul$xdata, ydata = simul$ydata,
  family = "gaussian"
)
# Calibration plot
CalibrationPlot(stab)
# Extracting the results
summary(stab)
Stable(stab)
SelectionProportions(stab)
plot(stab)
# Using randomised LASSO
stab <- VariableSelection(
  xdata = simul$xdata, ydata = simul$ydata,
  family = "gaussian", penalisation = "randomised"
)
plot(stab)
```

```
# Using adaptive LASSO
stab <- VariableSelection(
 xdata = simul$xdata, ydata = simul$ydata,
 family = "gaussian", penalisation = "adaptive"
\lambdaplot(stab)
# Using additional arguments from glmnet (e.g. penalty.factor)
stab <- VariableSelection(
  xdata = simul$xdata, ydata = simul$ydata, family = "gaussian",
  penalty.factor = c(rep(1, 45), rep(0, 5))\lambdahead(coef(stab))
# Using CART
if (requireNamespace("rpart", quietly = TRUE)) {
  stab <- VariableSelection(
   xdata = simul$xdata, ydata = simul$ydata,
   implementation = CART,
   family = "gaussian",
 )
 plot(stab)
}
# Regression with multivariate outcomes
set.seed(1)
simul \le SimulateRegression(n = 100, pk = 20, q = 3, family = "gaussian")
stab <- VariableSelection(
 xdata = simul$xdata, ydata = simul$ydata,
 family = "mgaussian"
\lambdasummary(stab)
# Logistic regression
set.seed(1)
simul \le SimulateRegression(n = 200, pk = 10, family = "binomial", ev_xy = 0.8)
stab <- VariableSelection(
  xdata = simul$xdata, ydata = simul$ydata,
  family = "binomial"
\lambdasummary(stab)
# Sparse PCA (1 component, see BiSelection for more components)
if (requireNamespace("elasticnet", quietly = TRUE)) {
  set.seed(1)
  simul <- SimulateComponents(pk = c(5, 3, 4))
  stab <- VariableSelection(
   xdata = simul$data,
   Lambda = seq_len(ncol(simul$data) - 1),
   implementation = SparsePCA
  \lambdaCalibrationPlot(stab, xlab = "")
  summary(stab)
```
}

```
# Sparse PLS (1 outcome, 1 component, see BiSelection for more options)
if (requireNamespace("sgPLS", quietly = TRUE)) {
  set.seed(1)
  simul \le SimulateRegression(n = 100, pk = 50, family = "gaussian")
  stab <- VariableSelection(
    xdata = simul$xdata, ydata = simul$ydata,
   Lambda = seq\_len(ncol(simul$xdata) - 1),
    implementation = SparsePLS, family = "gaussian"
  )
  CalibrationPlot(stab, xlab = "")
  SelectedVariables(stab)
}
# Group PLS (1 outcome, 1 component, see BiSelection for more options)
if (requireNamespace("sgPLS", quietly = TRUE)) {
  stab <- VariableSelection(
    xdata = simul$xdata, ydata = simul$ydata,
   Lambda = seq\_len(5),
   group_x = c(5, 5, 10, 20, 10),
   group_penalisation = TRUE,
   implementation = GroupPLS, family = "gaussian"
  )
  CalibrationPlot(stab, xlab = "")
  SelectedVariables(stab)
}
# Example with more hyper-parameters: elastic net
set.seed(1)
simul <- SimulateRegression(n = 100, pk = 50, family = "gaussian")
TuneElasticNet <- function(xdata, ydata, family, alpha) {
  stab <- VariableSelection(
   xdata = xdata, ydata = ydata,
    family = family, alpha = alpha, verbose = FALSE
  \lambdareturn(max(stab$S, na.rm = TRUE))
}
myopt <- optimise(TuneElasticNet,
  lower = 0.1, upper = 1, maximum = TRUE,
  xdata = simul$xdata, ydata = simul$ydata,
 family = "gaussian"
\lambdastab <- VariableSelection(
  xdata = simul$xdata, ydata = simul$ydata,
  family = "gaussian", alpha = myopt\$maximum\mathcal{L}summary(stab)
enet <- SelectedVariables(stab)
# Comparison with LASSO
stab <- VariableSelection(xdata = simul$xdata, ydata = simul$ydata, family = "gaussian")
summary(stab)
```

```
lasso <- SelectedVariables(stab)
table(lasso, enet)
# Example using an external function: group-LASSO with gglasso
if (requireNamespace("gglasso", quietly = TRUE)) {
 set.seed(1)
 simul \le SimulateRegression(n = 200, pk = 20, family = "binomial")
 ManualGridGroupLasso <- function(xdata, ydata, family, group_x, ...) {
    # Defining the grouping
   group <- do.call(c, lapply(seq_len(length(group_x)), FUN = function(i) {
      rep(i, group_x[i])
    }))
   if (family == "binomial") {
      ytmp <- ydata
      ytmp[ytmp == min(ytmp)] < -1ytmp[ytmp == max(ytmp)] \leftarrow 1return(gglasso::gglasso(xdata, ytmp, loss = "logit", group = group, ...))
   } else {
   return(gglasso::gglasso(xdata, ydata, lambda = lambda, loss = "ls", group = group, ...))
   }
 }
 Lambda <- LambdaGridRegression(
   xdata = simul$xdata, ydata = simul$ydata,
    family = "binomial", Lambda_cardinal = 20,
    implementation = ManualGridGroupLasso,
   group_x = rep(5, 4)\lambdaGroupLasso <- function(xdata, ydata, Lambda, family, group_x, ...) {
    # Defining the grouping
   group <- do.call(c, lapply(seq_len(length(group_x)), FUN = function(i) {
     rep(i, group_x[i])
   }))
    # Running the regression
    if (family == "binomial") {
      ytmp <- ydata
      ytmp[ytmp == min(ytmp)] < -1ytmp[ytmp == max(ytmp)] < -1mymodel <- gglasso::gglasso(xdata, ytmp, lambda = Lambda, loss = "logit", group = group, ...)
    }
    if (family == "gaussian") {
   mymodel <- gglasso::gglasso(xdata, ydata, lambda = Lambda, loss = "ls", group = group, ...)
    }
    # Extracting and formatting the beta coefficients
   beta_full <- t(as.matrix(mymodel$beta))
   beta_full <- beta_full[, colnames(xdata)]
    selected \le ifelse(beta_full != 0, yes = 1, no = 0)
   return(list(selected = selected, beta_full = beta_full))
 }
 stab <- VariableSelection(
```
WeightBoxplot 127

```
xdata = simul$xdata, ydata = simul$ydata,
    implementation = GroupLasso, family = "binomial", Lambda = Lambda,group_x = rep(5, 4),group_penalisation = TRUE
 )
 summary(stab)
}
par(oldpar)
```
WeightBoxplot *Stable attribute weights*

Description

Creates a boxplots of the distribution of (calibrated) median attribute weights obtained from the COSA algorithm across the subsampling iterations. See examples in [Clustering](#page-19-0).

Usage

```
WeightBoxplot(
  stability,
  at = NULL,argmax_id = NULL,
  col = NULL,boxwex = 0.3,
  xlab = ",
 ylab = "Weight",
 cex.1ab = 1.5,
  \text{las} = 3,
  frame = "F",
  add = FALSE,...
)
```
Arguments

Value

A boxplot.

See Also

[Clustering](#page-19-0)

Index

∗ clustering algorithms DBSCANClustering, [30](#page-29-0) GMMClustering, [40](#page-39-0) HierarchicalClustering, [55](#page-54-0) KMeansClustering, [60](#page-59-0) PAMClustering, [70](#page-69-0) ∗ ensemble model functions Ensemble, [32](#page-31-0) EnsemblePredictions, [33](#page-32-0) ∗ functions for model performance ClusteringPerformance, [25](#page-24-0) SelectionPerformance, [95](#page-94-0) SelectionPerformanceGraph, [96](#page-95-0) ∗ lambda grid functions LambdaGridGraphical, [61](#page-60-0) LambdaGridRegression, [64](#page-63-1) LambdaSequence, [66](#page-65-0) ∗ multi-block functions BlockLambdaGrid, [15](#page-14-0) ∗ penalised dimensionality reduction functions GroupPLS, [53](#page-52-0) SparseGroupPLS, [99](#page-98-0) SparsePCA, [101](#page-100-0) SparsePLS, [103](#page-102-0) ∗ prediction performance functions ExplanatoryPerformance, [34](#page-33-1) Incremental, [57](#page-56-1) ∗ stability functions BiSelection, [8](#page-7-1) Clustering, [20](#page-19-1) GraphicalModel, [46](#page-45-1) StructuralModel, [113](#page-112-1) VariableSelection, [118](#page-117-1) ∗ stability metric functions ConsensusScore, [29](#page-28-1) FDP, [38](#page-37-1) PFER, [77](#page-76-1) StabilityMetrics, [106](#page-105-1)

StabilityScore, [110](#page-109-1) ∗ underlying algorithm functions CART, [18](#page-17-0) ClusteringAlgo, [24](#page-23-0) PenalisedGraphical, [71](#page-70-0) PenalisedOpenMx, [73](#page-72-0) PenalisedRegression, [75](#page-74-1) ∗ wrapping functions GraphicalAlgo, [45](#page-44-0) SelectionAlgo, [93](#page-92-1) Adjacency, *[42](#page-41-0)*, *[51](#page-50-0)* Adjacency *(*Stable*)*, [111](#page-110-0) AggregatedEffects, [5](#page-4-0) Argmax, *[8](#page-7-1)* Argmax *(*ArgmaxId*)*, [7](#page-6-0) ArgmaxId, *[7](#page-6-0)*, [7,](#page-6-0) *[8](#page-7-1)* beep, *[11](#page-10-0)*, *[21](#page-20-0)*, *[49](#page-48-0)*, *[121](#page-120-0)* BiSelection, *[6](#page-5-0)*, [8,](#page-7-1) *[16](#page-15-1)[–18](#page-17-0)*, *[23](#page-22-0)*, *[44](#page-43-0)*, *[51](#page-50-0)*, *[54](#page-53-0)*, *[84](#page-83-0)*, *[89](#page-88-0)*, *[95](#page-94-0)*, *[97,](#page-96-0) [98](#page-97-0)*, *[100](#page-99-0)*, *[102](#page-101-0)*, *[104](#page-103-0)*, *[112](#page-111-0)*, *[117](#page-116-0)*, *[123](#page-122-0)* BlockLambdaGrid, [15](#page-14-0) BlockStructure, *[96](#page-95-0)* boxplot, *[127,](#page-126-0) [128](#page-127-0)* CalibrationPlot, *[11](#page-10-0)*, [16,](#page-15-1) *[22](#page-21-0)*, *[49](#page-48-0)*, *[115](#page-114-0)*, *[121](#page-120-0)* CART, [18,](#page-17-0) *[25](#page-24-0)*, *[72](#page-71-0)*, *[74](#page-73-0)*, *[76](#page-75-0)* Clustering, *[13](#page-12-0)*, *[16](#page-15-1)[–18](#page-17-0)*, [20,](#page-19-1) *[26,](#page-25-0) [27](#page-26-1)*, *[51](#page-50-0)*, *[78](#page-77-0)*, *[98](#page-97-0)*, *[112](#page-111-0)*, *[117](#page-116-0)*, *[123](#page-122-0)*, *[127,](#page-126-0) [128](#page-127-0)* ClusteringAlgo, *[19](#page-18-0)*, [24,](#page-23-0) *[72](#page-71-0)*, *[74](#page-73-0)*, *[76](#page-75-0)* ClusteringPerformance, [25,](#page-24-0) *[96,](#page-95-0) [97](#page-96-0)* Clusters, *[22](#page-21-0)*, *[26](#page-25-0)*, *[78](#page-77-0)* Clusters *(*Stable*)*, [111](#page-110-0) coef, *[36](#page-35-0)* Combine, [27,](#page-26-1) *[50](#page-49-0)*, *[116](#page-115-0)*, *[122](#page-121-0)* CoMembership, *[26](#page-25-0)*, [28](#page-27-0) concordance, *[36](#page-35-0)* ConsensusMatrix *(*SelectionProportions*)*, [98](#page-97-0)

130 INDEX

ConsensusScore, *[11](#page-10-0)*, *[22,](#page-21-0) [23](#page-22-0)*, [29,](#page-28-1) *[39](#page-38-0)*, *[49](#page-48-0)*, *[77](#page-76-1)*, *[109](#page-108-0)*, *[111](#page-110-0)*, *[115](#page-114-0)*, *[121](#page-120-0)* cosa2, *[20](#page-19-1)*, *[30,](#page-29-0) [31](#page-30-0)*, *[55,](#page-54-0) [56](#page-55-0)*, *[70](#page-69-0)* coxph, *[35](#page-34-0)*, *[58](#page-57-0)*, *[89](#page-88-0)* cv.glmnet, *[89](#page-88-0)* dbscan, *[20](#page-19-1)*, *[24](#page-23-0)*, *[30,](#page-29-0) [31](#page-30-0)* DBSCANClustering, [30,](#page-29-0) *[40](#page-39-0)*, *[56](#page-55-0)*, *[61](#page-60-0)*, *[71](#page-70-0)* dist, *[30,](#page-29-0) [31](#page-30-0)*, *[55,](#page-54-0) [56](#page-55-0)*, *[70](#page-69-0)* Ensemble, [32,](#page-31-0) *[33,](#page-32-0) [34](#page-33-1)*, *[85,](#page-84-0) [86](#page-85-0)* EnsemblePredictions, *[33](#page-32-0)*, [33,](#page-32-0) *[86](#page-85-0)* ExplanatoryPerformance, [34,](#page-33-1) *[57](#page-56-1)*, *[59](#page-58-0)*, *[80,](#page-79-0) [81](#page-80-0)*, *[123](#page-122-0)* FDP, *[30](#page-29-0)*, [38,](#page-37-1) *[77](#page-76-1)*, *[106](#page-105-1)*, *[109](#page-108-0)*, *[111](#page-110-0)*

Folds, [39](#page-38-0)

glassoFast, *[46](#page-45-1)*, *[48](#page-47-0)*, *[62,](#page-61-0) [63](#page-62-0)*, *[72](#page-71-0)* glm, *[35](#page-34-0)*, *[58](#page-57-0)*, *[89](#page-88-0)* glmnet, *[19](#page-18-0)*, *[39](#page-38-0)*, *[65](#page-64-0)*, *[73](#page-72-0)[–75](#page-74-1)*, *[92](#page-91-0)*, *[94](#page-93-0)*, *[105](#page-104-0)*, *[120](#page-119-0)* GMMClustering, *[21](#page-20-0)*, *[23,](#page-22-0) [24](#page-23-0)*, *[31](#page-30-0)*, [40,](#page-39-0) *[56](#page-55-0)*, *[61](#page-60-0)*, *[71](#page-70-0)* gPLS, *[54](#page-53-0)* gPLSda, *[54](#page-53-0)* Graph, [41,](#page-40-0) *[44](#page-43-0)*, *[50,](#page-49-0) [51](#page-50-0)*, *[97](#page-96-0)* graph_from_adjacency_matrix, *[42](#page-41-0)* GraphComparison, [43](#page-42-0) GraphicalAlgo, [45,](#page-44-0) *[51](#page-50-0)*, *[94](#page-93-0)* GraphicalModel, *[8](#page-7-1)*, *[13](#page-12-0)*, *[15–](#page-14-0)[18](#page-17-0)*, *[23](#page-22-0)*, *[27](#page-26-1)*, *[41,](#page-40-0) [42](#page-41-0)*, *[44](#page-43-0)*, *[46](#page-45-1)*, [46,](#page-45-1) *[72](#page-71-0)*, *[95](#page-94-0)*, *[97,](#page-96-0) [98](#page-97-0)*, *[112](#page-111-0)*, *[117](#page-116-0)*, *[123](#page-122-0)* GroupPLS, *[13](#page-12-0)*, [53,](#page-52-0) *[94](#page-93-0)*, *[100](#page-99-0)*, *[102](#page-101-0)*, *[104](#page-103-0)*

hclust, *[21](#page-20-0)*, *[55,](#page-54-0) [56](#page-55-0)*, *[78](#page-77-0)*, *[112](#page-111-0)* Heatmap, *[79](#page-78-0)* HierarchicalClustering, *[21](#page-20-0)*, *[23,](#page-22-0) [24](#page-23-0)*, *[31](#page-30-0)*, *[40](#page-39-0)*, [55,](#page-54-0) *[61](#page-60-0)*, *[71](#page-70-0)*

igraph, *[41,](#page-40-0) [42](#page-41-0)*, *[44](#page-43-0)*, *[50](#page-49-0)* Incremental, *[36](#page-35-0)*, [57,](#page-56-1) *[79,](#page-78-0) [80](#page-79-0)*, *[123](#page-122-0)* IncrementalPlot *(*plot.incremental*)*, [79](#page-78-0)

kmeans, *[60,](#page-59-0) [61](#page-60-0)* KMeansClustering, *[21](#page-20-0)*, *[23,](#page-22-0) [24](#page-23-0)*, *[31](#page-30-0)*, *[40](#page-39-0)*, *[56](#page-55-0)*, [60,](#page-59-0) *[71](#page-70-0)* KMeansSparseCluster, *[61](#page-60-0)*

LambdaGridGraphical, *[45](#page-44-0)*, *[47](#page-46-0)*, *[51](#page-50-0)*, [61,](#page-60-0) *[66](#page-65-0)* LambdaGridRegression, *[63](#page-62-0)*, [64,](#page-63-1) *[66](#page-65-0)*, *[94](#page-93-0)*, *[119](#page-118-0)*, *[123](#page-122-0)*

LambdaSequence, *[63](#page-62-0)*, *[66](#page-65-0)*, [66](#page-65-0) LinearSystemMatrix, [67,](#page-66-0) *[74](#page-73-0)* lm, *[35](#page-34-0)*, *[58](#page-57-0)*, *[89](#page-88-0)* Mclust, *[40](#page-39-0)* mean, *[6](#page-5-0)* median, *[6](#page-5-0)* multinom, *[35](#page-34-0)*, *[58](#page-57-0)*, *[89](#page-88-0)* multisession, *[10](#page-9-0)*, *[12](#page-11-0)*, *[21,](#page-20-0) [22](#page-21-0)*, *[49,](#page-48-0) [50](#page-49-0)*, *[115,](#page-114-0) [116](#page-115-0)*, *[121,](#page-120-0) [122](#page-121-0)* mxModel, *[68](#page-67-0)* mxPenaltySearch, *[67](#page-66-0)* mxRun, *[68](#page-67-0)* nloptr, *[21](#page-20-0)*, *[49](#page-48-0)*, *[114,](#page-113-0) [115](#page-114-0)*, *[120,](#page-119-0) [121](#page-120-0)* OpenMx, *[73,](#page-72-0) [74](#page-73-0)* OpenMxMatrix, [67,](#page-66-0) *[69](#page-68-0)*, *[74](#page-73-0)* OpenMxModel, *[68](#page-67-0)*, [68](#page-67-0) pam, *[70](#page-69-0)* PAMClustering, *[21](#page-20-0)*, *[23,](#page-22-0) [24](#page-23-0)*, *[31](#page-30-0)*, *[40](#page-39-0)*, *[56](#page-55-0)*, *[61](#page-60-0)*, [70](#page-69-0) par, *[17,](#page-16-0) [18](#page-17-0)*, *[79](#page-78-0)[–82](#page-81-0)*, *[128](#page-127-0)* PenalisedGraphical, *[19](#page-18-0)*, *[25](#page-24-0)*, *[46](#page-45-1)*, *[51](#page-50-0)*, [71,](#page-70-0) *[74](#page-73-0)*, *[76](#page-75-0)* PenalisedLinearSystem, *[67](#page-66-0)*, *[73,](#page-72-0) [74](#page-73-0)* PenalisedLinearSystem *(*PenalisedOpenMx*)*, [73](#page-72-0) PenalisedOpenMx, *[19](#page-18-0)*, *[25](#page-24-0)*, *[68,](#page-67-0) [69](#page-68-0)*, *[72,](#page-71-0) [73](#page-72-0)*, [73,](#page-72-0) *[74](#page-73-0)*, *[76](#page-75-0)* PenalisedRegression, *[19](#page-18-0)*, *[25](#page-24-0)*, *[72](#page-71-0)*, *[74](#page-73-0)*, [75,](#page-74-1) *[94](#page-93-0)*, *[123](#page-122-0)* PFER, *[30](#page-29-0)*, *[39](#page-38-0)*, [77,](#page-76-1) *[106](#page-105-1)*, *[109](#page-108-0)*, *[111](#page-110-0)* plot.clustering, [78](#page-77-0) plot.incremental, [79](#page-78-0) plot.roc_band, [80](#page-79-0) plot.variable_selection, [81](#page-80-0) PlotIncremental *(*plot.incremental*)*, [79](#page-78-0) PLS, [82,](#page-81-0) *[87](#page-86-0)[–89](#page-88-0)* pls, *[82,](#page-81-0) [83](#page-82-0)* points, *[17](#page-16-0)* predict, *[33](#page-32-0)*, *[85](#page-84-0)* predict.pls, *[87](#page-86-0)* predict.variable_selection, *[34](#page-33-1)*, [85](#page-84-0) PredictPLS, [87](#page-86-0)

RCy3, *[42](#page-41-0)* Recalibrate *(*Refit*)*, [88](#page-87-1) Refit, *[6](#page-5-0)*, *[36](#page-35-0)*, *[59](#page-58-0)*, *[85,](#page-84-0) [86](#page-85-0)*, [88,](#page-87-1) *[123](#page-122-0)*

$I₃₁$ is a set of I

Resample , *[13](#page-12-0)* , *[23](#page-22-0)* , *[51](#page-50-0)* , [91](#page-90-1) , *[117](#page-116-0)* , *[123](#page-122-0)* ROC , *[80](#page-79-0) , [81](#page-80-0)* rpart , *[18](#page-17-0) , [19](#page-18-0)* SelectedVariables *(*Stable *)* , [111](#page-110-0) SelectionAlgo , *[19](#page-18-0)* , *[46](#page-45-1)* , *[74](#page-73-0)* , *[76](#page-75-0)* , [93](#page-92-1) , *[117](#page-116-0)* , *[123](#page-122-0)* SelectionPerformance , *[26](#page-25-0)* , [95](#page-94-0) , *[97](#page-96-0)* SelectionPerformanceGraph , *[26](#page-25-0)* , *[44](#page-43-0)* , *[96](#page-95-0)* , [96](#page-95-0) SelectionProportions , [98](#page-97-0) set.seed , *[10](#page-9-0)* , *[21](#page-20-0)* , *[48](#page-47-0)* , *[65](#page-64-0)* , *[89](#page-88-0)* , *[114](#page-113-0)* , *[119](#page-118-0)* sgPLS , *[54](#page-53-0)* , *[99](#page-98-0) , [100](#page-99-0)* sgPLSda , *[99](#page-98-0) , [100](#page-99-0)* sharp-package, [3](#page-2-0) SimulateClustering , *[26](#page-25-0)* SimulateComponents , *[95](#page-94-0)* SimulateGraphical , *[44](#page-43-0)* , *[95](#page-94-0)* , *[97](#page-96-0)* SimulateRegression , *[44](#page-43-0)* , *[95](#page-94-0)* , *[97](#page-96-0)* SparseGroupPLS , *[13](#page-12-0)* , *[54](#page-53-0)* , *[94](#page-93-0)* , [99](#page-98-0) , *[102](#page-101-0)* , *[104](#page-103-0)* SparsePCA , *[13](#page-12-0)* , *[54](#page-53-0)* , *[94](#page-93-0)* , *[100](#page-99-0)* , [101](#page-100-0) , *[104](#page-103-0)* SparsePLS , *[13](#page-12-0)* , *[54](#page-53-0)* , *[94](#page-93-0)* , *[100](#page-99-0)* , *[102](#page-101-0)* , [103](#page-102-0) spca , *[101](#page-100-0) , [102](#page-101-0)* Split , [105](#page-104-0) sPLS , *[103](#page-102-0)* sPLSda , *[103](#page-102-0)* Square, [106](#page-105-1) StabilityMetrics , *[30](#page-29-0)* , *[39](#page-38-0)* , *[77](#page-76-1)* , [106](#page-105-1) , *[111](#page-110-0)* StabilityScore , *[11](#page-10-0)* , *[13](#page-12-0)* , *[30](#page-29-0)* , *[39](#page-38-0)* , *[49](#page-48-0)* , *[51](#page-50-0)* , *[77](#page-76-1)* , *[106](#page-105-1)* , *[109](#page-108-0)* , [110](#page-109-1) , *[115](#page-114-0)* , *[117](#page-116-0)* , *[121](#page-120-0)* , *[123](#page-122-0)* Stable, [111](#page-110-0) StructuralModel , *[13](#page-12-0)* , *[23](#page-22-0)* , *[51](#page-50-0)* , [113](#page-112-1) , *[123](#page-122-0)* text , *[18](#page-17-0)*

VariableSelection , *[6](#page-5-0)* , *[8](#page-7-1)* , *[13](#page-12-0)* , *[16–](#page-15-1)[19](#page-18-0)* , *[23](#page-22-0)* , *[25](#page-24-0)* , *[27](#page-26-1)* , *[32](#page-31-0) , [33](#page-32-0)* , *[35](#page-34-0) , [36](#page-35-0)* , *[44](#page-43-0)* , *[51](#page-50-0)* , *[54](#page-53-0)* , *[58](#page-57-0) , [59](#page-58-0)* , *[74](#page-73-0)* , *[76](#page-75-0)* , *[81](#page-80-0) , [82](#page-81-0)* , *[84](#page-83-0) , [85](#page-84-0)* , *[89](#page-88-0)* , *[94](#page-93-0) , [95](#page-94-0)* , *[97,](#page-96-0) [98](#page-97-0)* , *[100](#page-99-0)* , *[102](#page-101-0)* , *[104](#page-103-0)* , *[112](#page-111-0)* , *[117](#page-116-0)* , [118](#page-117-1) visNetwork , *[42](#page-41-0)* , *[50](#page-49-0)*

WeightBoxplot , [127](#page-126-0)